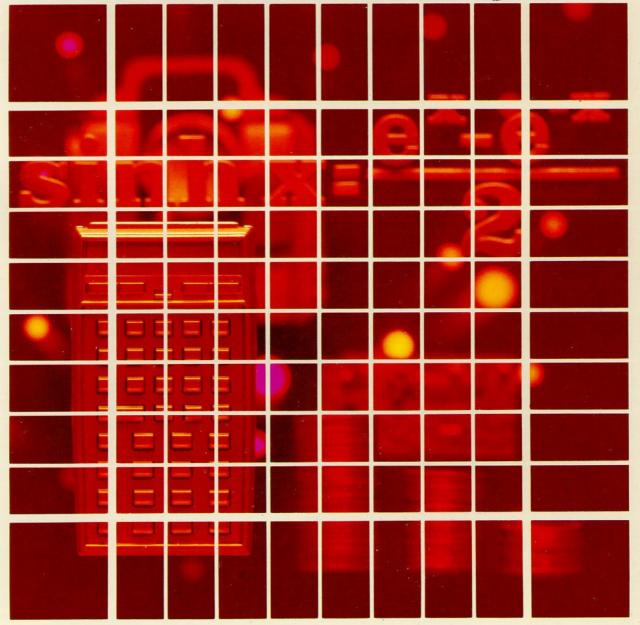
HP-41C

USERS'
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Business Stat/Marketing/Sales



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INTRODUCTION

This HP-41C Solutions book was written to help you get the most from your calculator. The programs were chosen to provide useful calculations for many of the common problems encountered.

They will provide you with immediate capabilities in your everyday calculations and you will find them useful as guides to programming techniques for writing your own customized software. The comments on each program listing describe the approach used to reach the solution and help you follow the programmer's logic as you become and expert on your HP calculator.

KEYING A PROGRAM INTO THE HP-41C

There are several things that you should keep in mind while you are keying in programs from the program listings provided in this book. The output from the HP 82143A printer provides a convenient way of listing and an easily understood method of keying in programs without showing every keystroke. This type of output is what appears in this handbook. Once you understand the procedure for keying programs in from the printed listings, you will find this method simple and fast. Here is the procedure:

1. At the end of each program listing is a listing of status information required to properly execute that program. Included is the SIZE allocation required. Before you begin keying in the program, press XEQ ALPHA SIZE ALPHA and specify the allocation (three digits; e.g., 10 should be specified as 010).

Also included in the status information is the display format and status of flags important to the program. To ensure proper execution, check to see that the display status of the HP-41C is set as specified and check to see that all applicable flags are set or clear as specified.

- 2. Set the HP-41C to PRGM mode (press the PRGM key) and press GTO to prepare the calculator for the new program.
- 3. Begin keying in the program. Following is a list of hints that will help you when you key in your programs from the program listings in this handbook.
 - a. When you see "(quote marks) around a character or group of characters in the program listing, those characters are ALPHA. To key them in, simply press ALPHA, key in the characters, then press ALPHA again. So "SAMPLE" would be keyed in as ALPHA "SAMPLE" ALPHA.
 - b. The diamond in front of each LBL instruction is only a visual aid to help you locate labels in the program listings. When you key in a program, ignore the diamond.
 - c. The printer indication of divide sign is /. When you see / in the program listing, press + .
 - d. The printer indication of the multiply sign is # . When you see # in the program listing, press 🗷.
 - e. The f- character in the program listing is an indication of the APPEND function. When you see f-, press APPEND in ALPHA mode (press and the K key).
 - f. All operations requiring register addresses accept those addresses in these forms:

```
nn (a two-digit number)
IND nn (INDIRECT: , followed fy a two-digit number)
X, Y, Z, T, or L (a STACK address: followed by X, Y, Z, T, or L)
IND X, Y, Z, T or L (INDIRECT stack: followed by X, Y, Z, T, or L)
```

Indirect addresses are specified by pressing and then the indirect address. Stack addresses are specified by pressing followed by X, Y, Z, T, or L. Indirect stack addresses are specified by pressing and X, Y, Z, T, or L.

Printer Listing Kevstrokes **Display** LBL ALPHA SAMPLE ALPHA 01 LBLTSAMPLE Ø1+LBL "SAM PLE" ALPHA THIS IS A ALPHA 02THIS IS A 02 "THIS IS ALPHA APPEND SAMPLE 03[™] ⊢ SAMPLE 03 "ESAMPLE AVIEW (ALPHA) 04 AVIEW **04 AVIEW** 05 6 **95** 6 ENTER+ 06 ENTER / 06 ENTERT 2 [CHS] **0**7 −2 **0**8 ∠ 07 - 2÷ 08 / **09 ABS** XEQ ALPHA ABS ALPHA 09 ABS 10 STO IND STO . 10 STO IND L 11 "83=" ALPHA R3= ARCL 03 11^TR3= 12 ARCL 03 AVIEW 13 AVIEW 12 ARCL 03 **14 RTN** ALPHA 13 AVIEW RTN **14 RTN**

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FORECASTING USING EXPONENTIAL SMOOTHING

Exponential smoothing is a special kind of moving average. It is often used for short-term sales and inventory forecasts. Typical forecast periods are monthly or quarterly.

Unlike a moving average, exponential smoothing does not require a great deal of historical data. This program, for example, forecasts demand by using only a smoothing constant, an "old smoothed average," and a current-period usage statistic.

This program is a singly-smoothed exponential forecasting routine which: (1) accomodates quarterly seasonal correction factors, (2) can handle some trend in the data, (3) produces smoothed estimates of current demand, D_t , (4) produces next-period smoothed demand estimates, D_{t+1} , (5) calculates a mean absolute deviation, MD, and a tracking ratio, T, (6) provides a goodness of fit measure, V, which measures the variance between the next period's demand estimate to that period's actual demand, and (7) provides for convenient restarting when the user wishes to update a data series.

This program should not be used with data which has more than a moderate amount of up or down trend. And, at least two projections of D $_{\rm t}$ + 1 be done before MD or T can be calculated.

Counter Q_i is used with the deseasonalizing adjustment option. Q_i keeps track of the fiscal quarter or calendar quarter associated with a given X_t , and should always be for time period t-1.

Equations:

$$\alpha$$
 = smoothing constant (0 < α < 1)

 X_{t} = actual current period usage smoothed average,

$$S_{t} = \alpha X_{t} + (1-\alpha)S_{t-1}$$

change,
$$C_t = S_t - S_{t-1}$$

trend,
$$T_t = \alpha C_t + (1 - \alpha) T_{t-1}$$

current period expected usage, $D_t = S_t + \frac{(1 - \alpha)}{\alpha} T_t$

forecase of next period expected usage, $D_{t+1} = S_t + (\frac{1}{\alpha}) T_t$

error,
$$e = D_t - X_t$$

cumulative error =
$$\sum_{t=1}^{m} e^2$$

initial conditions: $S_{t-1} = X_{t-1}$

$$T_{t-1} = 0$$

SV = seasonal variation factor

1

References:

HP-67/97 Users' Library program #01206D written by Professor Robert Olsen.

Robert Goodell Brown, <u>Smoothing</u>, <u>Forecasting</u>, <u>and Prediction of Discrete Time</u> Series, Englewood Cliffs, New Jersey: Prentice-Hall, 1963.

Elwood S. Buffa and William H. Taubert, <u>Production-Inventory Systems</u>:

<u>Planning and Control</u>, Rev. ed., Homewood, Illinois: Richard D. Irwin, 1972.

Norbert Lloyd Enrick, <u>Market and Sales Forecasting</u>, San Francisco, California: Chandler Publishing Co., 1969.

Example:

Test Data when deseasonalization done.

Time Period	Actual X _t
0	100
1	100
2	150
3	70

 $\alpha = 0.2 \text{ Q}_0 = 4$, SV₁=1.15, SV₂=0.94, SV₃=0.89, SV₄=1.02

Keystrokes:	Display:
[USER]	(Set USER mode)
[XEQ] [ALPHA] SIZE [ALPHA] 023	
[XEQ] [ALPHA] SMOOTH [ALPHA]	ALPHA=?
.2 [R/S]	0.00
1.15 [ENTER†] .94 [ENTER†]	
.89 [ENTER↑] 1.02 [///] [B]	1.02
4 [ENTER†] 100 [A]	102.00
100 [B]	B=1
[R/S]	D1=106.68 (Deseasonalized smoothed D_t)
[R/S]	SD1=92.77 (Seasonalized smoothed D_t)
[R/S]	D2 [†] =107.20 (Deseasonalized forecast)
[R/S]	SD2 [†] =114.04 (Seasonalized forecast)

Keystrokes:

150 [B]

[R/S]

[R/S]

[R/S]

[R/S]

[C]

[R/S]

[R/S]

[R/S]

[R/S]

70 [B]

[R/S]

[R/S]

[R/S]

[R/S]

[C]

[R/S]

[R/S]

[R/S]

[R/S]

Display:

B=2

D2=119.37

SD2=126.99

 $D3\uparrow=121.24$

 $SD3\uparrow = 136.22$

MD = 33.80

T=1.00

 $\Sigma e2 = 1142.44$

B=2.00

V = 571.22

B=3

D3=100.02

SD3=112.38

 $D4 \uparrow = 99.54$

 $SD4\uparrow = 97.58$

MD = 46.37

T = -0.54

 $\Sigma e2 = 4616.36$

B=3.00

V=1538.79

User Instructions

P INSTRUCTIONS	INPUT	FUNCTION	DICRIAY
		1011011011	DISPLAY
Load program and set USER mode		[USER]	4,000
Initialize		[XEQ] SMOOTH	ALPHA=?
Key in value of alpha	α	[R/S]	0.00
(Optional) Key in seasonal coefficien	nts SV ₃	[ENTERT]	SV
	SV ₂	[ENTER+]	SV ₂
	SV ₃	[ENTER]	SV ₃
	SV ₄	[///] [В]	SV ₄
(Optional) Store T_{t-1} if known.	T _t	[STO] 04	T _{t-1}
Key in Q_i for T_{t-1} , X_{t-1} (or S_{t-1} if	known) Q _i	[ENTER]	Qi
	x _{t-1}	[A]	x_{t-1} (D)
Key in X _t and calculate expected cur	rent		
usage	X _t	[B]	B=t _n
		[R/S]	Dt =
Calculate expected seasonalized curr	ent		
usage		[R/S]	SDt =
Calculate D_{t+1} and set up calculation	ns for		
MD, T and V		[R/S]	Dt _{n+1} =
		[R/S]	$SDt_{n+1} =$
. Calculate MD, T, ∑e _i , V		[c]	MD=
		[R/S]	T=
		[R/S]	Σe2=
		[R/S]	B=
		[R/S]	V=
. Continue keying in data using steps	7-9,		
repeating step 10 as often as desire			

4

01+LBL "SMO		50 9	
OTH"	Initialize	51 +	
02 SF 21		52 RDN	
03 CF 29		53 RCL IND	Į.
04 CLRG			
		Τ	
,		54 *	
06 STO 10		55 STO 22	
07 STO 11		56 i	
08 STO 12		57 ST+ 09	
09 STO 13		58 "B="	
10 "ALPHA=?	1	59 XEQ 02	
		60 AVIEW	
11 PROMPT			
12 STO 18	~ → P	61 1	
i e	$\alpha \rightarrow R_{18}$	62 RCL 09	
13	1	63 X=Y?	
14 STO 19	$1-\alpha\rightarrow R_{19}$	64 GTO 01	
15 CLX	İ	65 RCL 22	Prior period
16 RTN	1	66 RCL 17	estimate D t+1(I)
17+LBL b		67 -	1 (1)
18 STO 13	Enter SV's	68 ST+ 14	
19 RDN	Elicel SV S	69 STO 16	
20 STO 12			
I and the second		70 ASS	
21 RDN		71 ST+ 15	
22 STO 11		72 X12	
23 RDN		73 ST+ 03	Σe_{i}^{2}
24 STO 10		74+LBL 01	1
25 RDN		75 RCL 19	
26 RTH		76 RCL 01	Calculate
27+LBL A		77 *	Calculate S _{t(D)}
28 STO 20	ŀ	78 RCL 18	1
29 X<>Y	Enter start-up		1
ຊ້ອ໌ ຣິກັດ ອຣ	data	79 RCL 22	.
		80 STO 21	
31 9		81 *	
32 +		82 +	
33 RDN		83 STO 02	
34 RCL IND		84 RCL 01	Calculate C _{t(D)}
Ŧ		85 -	(0)
35 *		86 RCL 18	
36 STO 21		87 *	
37 STO 01		88 RCL 04	
38 RTN			Coloulata
39+LBL B	Enter Y	89 RCL 19	Calculate T _{t(D)}
	Enter X t	90 *	, ,
40 STO 00		91 +	
41 RCL 08		92 STO 04	
42 4		93 RCL 19	
43 /		94 RCL 18	Calculate D _{t(D)}
44 FRC		95 /	t(D)
45 4		96 *	
46 *		97 RCL 02	
47 1	·	98 STO 01	1
48 +	·	38 4	Į į
<u>49 STO 08</u>			1
<u> </u>		100 STO 06	

101 XEQ 93 102 XEQ 90 103 RCL 08 104 9 105 + 106 RCL 06 107 RCL IND	Calculate D _t (S)	151 "B" 152 RCL 09 153 XEQ 00 154 / 155 "V" 156+LBL 00 157 "H=" 158 ARCL X	V Output routine
108 / 109 "SD" 110 XEQ 02 111 XEQ 00 112 1 113 ST+ 09 114 RCL 02 115 RCL 04 116 RCL 18	Calculate D _{t+1}	159 AVIEW 160 RTN 161*LBL 03 162 "B" 163*LBL 02 164 FIX 0 165 ARCL 09 166 FIX 2 167 .END.	
117 / 118 + 119 XEQ 03 120 "H1" 121 XEQ 00 122 STO 17 123 RCL 08 124 10 125 + 126 RCL 17		70	
127 RCL IND Y 128 / 129 "SD" 130 XEQ 02 131 "HT" 132 1 133 ST- 09 134 RDN	Calculate Dt+l(S) 80	
135 GTO 00 136*LBL C 137 RCL 14 138 RCL 15 139 RCL 09 140 1 141 - 142 / 143 "MD" 144 XEQ 00	Calculate MD	90	
145 / 146 "T" 147 XEQ 00 148 RCL 03	Calculate T		
149 "Σe2" 150 XEQ 00	Σe ²	00	

REGISTERS, STATUS, FLAGS, ASSIGNMENTS

DATA REGISTERS		A REGISTERS	STATUS
00	Xt St_1 St Σei^2	50	SIZE
05	Tt	55	INIT
	Dt		# S/C SET INDICATES CLEAR INDICATES
			21 Printer enable
	Qi		29 Suppress decimal
10	Bi SV ₁	60	
-	SV ₂	- 100	
-	SV ₃		
- 1	SV 4		
-+	CFE		
15	CAD	65	
-	Temp ei		
-1	Dt+1		
T I	α		
1	1-α		
20	Xt-1 (s)	70	
	Xt-1 (D)		
	Xt (D)		
25		75	
30			
30		80	
\dashv			
			
35		85	
 +			
			ASSIGNMENTS
_		100	FUNCTION KEY FUNCTION KEY
40		90	
\rightarrow			
+			
-+			
15		95	
-+			
\dashv			
+			
			i 1 1

MONTHLY SEASONAL VARIATION FACTORS BASED ON CENTERED MOVING AVERAGES

Seasonal variation factors are a useful concept in many types of forecasting. There are several methods of developing seasonal moving averages, one of the more common ways being to calculate them as the ratio of the periodic value to a centered moving average for the same period.

For instance, to determine the sales for the 7th month of a given year, a centered moving average for that month would be calculated from sales figures from the 1st thru 12th months of that year and the 1st month of the following year. The seasonal variation factor for the 7th month would then be the ratio of the actual sales in the 7th month to the centered moving average for that month.

Equations:

$$\overline{X}_{c} = \frac{X_{1}}{2} + (X_{2} + X_{3} + \dots + X_{m}) + \frac{X_{m} + 1}{2}$$

$$SV = \frac{X_{i}}{X_{i}}$$

where \overline{X}_{c} = centered moving average

m = number of elements in the centered moving average

SV = seasonal variation factor

 X_i = value of the ith data point

 \overline{X}_{i} = centered moving average of the data point

Example:

Econo-Wise Home Appliance Company's monthly sales for the last 15 months are:

Month	Sales (\$K)	Month	Sales (\$K)
1	397	9	513
2	376	10	434
3	460	11	56 2
4	501	12	593
5	455	13	579
6	390	14	601
7	530	15	598
8	560		

Find the centered 12-month moving average and seasonal variation factor for months 7-9.

Keystrokes:	Display
[XEQ] [ALPHA] SIZE [ALPHA] 014	
[XEQ] [ALPHA] SV [ALPHA]	MONTH 1=?
397 [R/S] 376 [R/S]	
460 [R/S] 501 [R/S]	
455 [R/S] 390 [R/S]	
530 [R/S] 560 [R/S]	
513 [R/S] 434 [R/S]	
562 [R/S] 593 [R/S]	MONTH 13=?
579 [R/S]	AVG=488.50 (Centered average for month 7)
[R/S]	SV%=108.50 (Seasonal variation factor)
[R/S]	NEXT MONTH=?
601 [R/S]	AVG=505.46 (Centered average for month 8)
[R/S]	SV%=110.79 (Seasonal variation factor)
[R/S]	NEXT MONTH=?
598 [R/S]	AVG=520.58 (Centered average for month 9)
[R/S]	SV%=98.54 (Seasonal variation factor)

User Instructions

SIZE: 014

] 0,22.014
STEP	INSTRUCTIONS	INPUT	FUNCTION	DISPLAY
1.	Load program			
2.	Initialize		[XEQ] SV	MONTH 1=?
3.	Key in 1st month sales	lst	[R/S]	MONTH 2=?
4.	Key in 2nd month sales	2nd	[R/S]	MONTH 3=?
5.	Repeat until month 13 sales are entered	13th		
6.	Calculate moving average for month 7		[R/S]	AVG =
7.	Calculate seasonal variation factor		[R/S]	SV% =
8.	Press [R/S] for next prompt.		[R/S]	NEXT MONTH=?
9.	Key in 14th month sales	14th		
10.	Calculate moving average for month 8.		[R/S]	AVG =
11.	Calculate seasonal variation factor		[R/S]	SV% =
12.	Press [R/S] for next prompt.		[R/S]	NEXT MONTH=?
13.	Repeat steps 9-12 for the balance of the			
	data.			
L	<u> </u>		L	

01+LBL "SV" 02 SF 21 03 12 04 STO 00 05 1 05 1 06+LBL 00 07 FIX 0 08 CF 29 09 "MONTH 10 ARCL X 11 "H=?" 12 PROMPT 13 FIX 2 14 SF 29 15 STO IND Y RDN 17 1 18 + 19 13 20 X<>Y 21 X<=Y? 22 GTO 00 23+LBL 01 24 RCL 02 23 *LBL 01 24 RCL 02 25 STO 09 55 STO 10 56 + 57 RCL 12 58 STO 11 59 RCL 12 58 STO 11 59 RCL 12 58 RCL 12 69 RCL 13 61 STO 12 62 RCL 00 64 + 65 RCL 00 66 / 67 "AVC=" 69 AVIEW 70 RCL 06 64 / 71 X<>Y 72 / 72 / 72 / 72 / 72 / 72 / 72 / 72 /
49 STO 08 50 + 00

REGISTERS, STATUS, FLAGS, ASSIGNMENTS

DATA REGISTERS				STATUS				
00	X ₁ X ₂	50	EN	G	FIX _	SCI	2 USER ON	MODE OFF _X
05	Х ₃ Х ₄ Х ₅	55		FLAGS INIT # S/C SET INDICATES				ND104750
	X ₆		21			nDICATES r enable		NDICATES
	X ₈ X ₉							
10	X ₁₀ X ₁₁	60						
	X ₁₂ X ₁₃							
15		65						
								٠
20		70						
-								
25		75						
30		80						
35		85						
						ASSIGN	IMENTS	
40		90		FUNC	TION	KEY	FUNCTION	KEY
40		30						
-								
45		95						

MULTIPLE LINEAR REGRESSION

This program performs a least squares multiple linear regression for a series of data points x, y, z. Linear regression is a statistical method for finding a straight line that best fits a set of data points. The equation of this straight line expresses the linear relationship between independent (x and y) and dependent (z) variables and is of the form:

$$z = a + bx + cy$$

The three variables are input by pressing [A]. If one or more of the data points was entered incorrectly, simply re-enter the incorrect value(s) and press [///] [A]. Then continue as before. The three coefficients (a, b, c) are calculated by pressing [B].

In addition, the program also calculates the coefficient of determination r^2 ([C]). This is an indication of the "goodness of fit" for the calculated straight line, and is a number between 0 and 1. Values closer to 1 indicate "better" fits than values closer to 0.

Having determined the equation (the [B]key), the user can then project estimates of z for given x, y values ([D]). The sums (Σx_i ; Σy_i ; Σz_i), the sums of squares (Σx_i^2 ; Σy_i^2 ; Σz_i^2), and the sums of cross products ($\Sigma x_i y_i$; $\Sigma x_i z_i$; $\Sigma y_i z_i$) are stored in registers 07-09, 04-06, and 01-03 respectively.

Equations:

$$z = a + bx + cy$$

$$\Sigma z_{i} = an + b\Sigma x_{i} + c\Sigma y_{i} \qquad i = 1, 2, ..., n$$

$$\Sigma x_{i} z_{i} = a\Sigma x_{i} + b\Sigma x_{i}^{2} + c\Sigma x_{i} y_{i}$$

$$\Sigma y_{i} z_{i} = a\Sigma y_{i} + b\Sigma x_{i} y_{i} + c\Sigma y_{i}^{2}$$

$$c = \frac{A - B}{[n\Sigma x_{i}^{2} - (\Sigma x_{i})^{2}][n\Sigma y_{i}^{2} - (\Sigma y_{i})^{2}] - [n\Sigma x_{i} y_{i} - (\Sigma x_{i})(\Sigma y_{i})]^{2}}$$

where:

$$A = [n\Sigma x_{i}^{2} - (\Sigma x_{i})^{2}] [n\Sigma y_{i}z_{i} - (\Sigma y_{i}) (\Sigma z_{i})]$$

$$B = [n\Sigma x_{i}y_{i} - (\Sigma x_{i}) (\Sigma y_{i})] [n\Sigma x_{i}z_{i} - (\Sigma x_{i}) (\Sigma z_{i})]$$

$$b = \frac{[n\Sigma x_{i}z_{i} - (\Sigma x_{i}) (\Sigma z_{i})] - c[n\Sigma x_{i}y_{i} - (\Sigma x_{i}) (\Sigma y_{i})]}{n\Sigma x_{i}^{2} - (\Sigma x_{i})^{2}}$$

$$\mathbf{a} = \frac{1}{n} \left(\Sigma \mathbf{z_i} - \mathbf{c} \, \Sigma \mathbf{y_i} - \mathbf{b} \, \Sigma \mathbf{x_i} \right)$$

$$\mathbf{R}^2 = \frac{\mathbf{a} \Sigma \mathbf{z_i} + \mathbf{b} \Sigma \mathbf{x_i} \mathbf{z_i} + \mathbf{c} \Sigma \mathbf{y_i} \mathbf{z_i} - \frac{1}{n} \left(\Sigma \mathbf{z_i} \right)^2}{\left(\Sigma \mathbf{z_i}^2 \right) - \frac{\left(\Sigma \mathbf{z_i} \right)^2}{n}}$$

Example:

A commercial land appraiser has examined 5 vacant lots in the downtown section of a local community, all of which have different depths, frontages, and values as shown below. Based on this data, what is the relationship between depth, frontage, and lot value? What is the coefficient of determination? What predicted value would a lot have with 50 foot depth and 70 foot frontage? With a 75 foot depth and 80 foot frontage?

Lot Depth (feet)	Lot Frontage (feet)	Lot Value
70	70.8	\$101,000
90	60.0	82,190
85	90.0	170,000
40	70.0	100,000
100	60.0	90,000

Keystrokes:	Display:
[USER]	(set USER mode)
[XEQ] [ALPHA] SIZE [ALPHA] 015	,
[XEQ] [ALPHA] MULT [ALPHA]	0.00
70 [ENTER†] 70.8 [ENTER†]	
101000 [A]	N=1.00
90 [ENTER†] 60 [ENTER†]	
82190 [A]	N=2.00
85 [ENTER†] 90 [ENTER†]	
170000 [A]	N=3.00
40 [ENTER+] 70 [ENTER+]	
100000 [A]	N=4.00
100 [ENTER†] 60 [ENTER†]	
90000 [A]	N=5.00
[B]	a=-118,499.03
[R/S]	b=314.71
[R/S]	c=2,892.02
[C]	R2=0.98
50 [ENTER†] 70 [D]	Z=99,678.08
75 [ENTER†] 80 [D]	Z=136,466.08

User Instructions

SIZE: 015

				0122 013
STEP	INSTRUCTIONS	INPUT	FUNCTION	DISPLAY
1.	Load program and set USER mode		[USER]	
2.	Initialize		[XEQ] MULT	0.00
3.	Key in x, y and corresponding z value	x	[ENTER†]	
		у	[ENTER†]	
		z	[A]	N=
4.	Repeat step 3 for all data			
5.	If data was input incorrectly, re-enter			
	incorrect x, y and z values.	x	[ENTER↑]	
		У	[ENTER†]	
		z	[///] [A]	N=
6.	Calculate coefficients.		[B]	a=
			[R/S]	b=
			[R/S]	c=
7.	Calculate coefficient of determination(r ²)		[c]	R2=
8.	Key in x and y values and calculate the			
	estimated z value, ĉ, displayed as			
	Z† (repeat as often as desired)	х	[ENTER↑]	
		у	[D]	Z †=
9.	For a new case, go to step 2.			
				-

$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	or
7"	01
02 FIX 2 53 FS? 01 Σx _i ,	
G7 CE 71 1 74 LMS	
04 CLRG 55 ST+ IND Σx, 2,	
05 CF 01 14	
06 CLX 56 RCL 14	
97 RTN 57 3	
08+LBL A 58 -	
09 STO 12 Input x _i ,y _i ,z _i 59 STO 14	
10 RDN 1"1" 60 RDN	
11 STO 11 61 X+2	
12 RDN 62 FS? 01	
13 STO 10 63 CHS	
14 7 64 ST+ IND	
15 STO 14 Compute 14	
16 RDN 65 RTN	
L couloulata a	Ъ,
17 XEQ 01 \(\Sigma_{\text{x}}\), \(\Sigma_{\text{y}}\), \(\Sigma_{\text{z}}\) 66 \(\Delta \) EL B calculate a \(\Delta \) 18 8 67 RCL 00	С
10 0T0 44	
20 RCL 11	
21 XEQ 01 70 RCL 07	
34 040	
$\begin{bmatrix} 22 & 9 \\ 23 & STO & 14 \end{bmatrix} \begin{bmatrix} \Sigma x_i y_i, \Sigma y_i z_i, & 72 & 72 & 72 & 72 & 72 & 72 & 72 & 7$	
04 pc; 40 73 STO 13	
25 XEQ 01 \(\Siz_i \text{x}\) 74 RCL 00	
26 RCL 10 75 RCL 03	
27 RCL 11 76 *	
28 * 77 RCL 08	
29 FS? 01 78 RCL 09	
30 CHS 79 *	
31 ST+ 01 80 -	
32 RCL 10 81 *	
33 RCL 12 82 STO 12	
34 * 83 RCL 00	
35 FS? 01 84 RCL 01	
36 CHS 85 *	
37 ST+ 02 86 RCL 07	
38 RCL 11 87 RCL 08	
39 RCL 12 88 *	
40 *	
41 FS? 01 90 STO 10	
42 CHS 91 RCL 00	
43 ST+ 03 92 RCL 02	
44 1 93 *	
45 FS?C 01 94 RCL 07	
46 CHS 95 RCL 09	
47 ST+ 00 96 *	
48 RCL 00 97 -	
49 "N=" 98 STO 11	
50 ARCL X 99 *	

100 RCL 12		152 RCL 12	
101 X<>Y		153 RCL 03	
102 -		154 *	1
103 RCL 13		155 +	
104 RCL 00	}	156 RCL 09	
105 RCL 05		157 X†2	
106 *		158 RCL 00	
107 RCL 08		159 /	
108 XT2			
109 -			
110 *			
111 RCL 10	1		
112 X12	l	163 X12	
113 -	•	164 RCL 00	
114 /		165 /	
115 STO 12	$c \rightarrow R_{12}$	166 -	
116 RCL 11	2 12	167 /	
117 RCL 10		168 "R2"	
118 RCL 18		169 GTO 00	^
		170+LBL D	Calculate z
	1	171 RCL 12	for given x, y
120 -		172 *	
121 RCL 13	1	173 X<>Y	
122 /	$b \rightarrow R_{11}$	174 RCL 11	
123 STO 11		175 *	
124 RCL 09		176 +	<u> </u>
125 RCL 12		177 RCL 10	1
126 RCL 08		178 +	
127 *		179 "Z*"	
128 -		180 GTO 02	:
129 RCL 11		181+LBL a	
130 RCL 07		182 SF 01	Correction of
131 *		183 GTO A	input values
132 -		184+LBL 00	l Impac variety
133 RCL 00		185 ADV	Output routine
134 /	$a \rightarrow R_{10}$	186+LBL 02	Jucput Toutine
135 STO 10	l a ' KIO	187 "⊢="	
136 "a"		188 ARCL X	
137 XEQ 00		189 AVIEW	
138 RCL 11		190 .END.	
139 "b"			
140 XEQ 02		90]
141 RCL 12			
142 "c"			
143 GTO 02			1
144+LBL C	Calculate r ²		
145 RCL 10	Jarcarace 1		1
146 RCL 09			
147 *			
148 RCL 11			
149 RCL 02			
150 *		00	-
151 +		00	
			`

REGISTERS, STATUS, FLAGS, ASSIGNMENTS

DATA REGISTERS		STATUS								
00	$ \begin{array}{c c} n \\ \Sigma x_{i} y_{i} \\ \Sigma x_{i} z_{i} \\ \overline{\Sigma y_{i} z_{i}} \\ \hline \Sigma y_{i} z_{i} \end{array} $	50	SIZE ENG DEG	015	5 TOT. — FIX – — RAD.	. REG	. <u>50</u> SCI GRAD		USER N	MODE _ OFF
05	Σy _i 2 2	55	#	INIT S/C	SET I		FLAG		CLEAR IN	IDICATES
	Σx _i Σy _i Σz _i		 01 21		correc Printer					
10	x _{ij} a y _{ij} b z _{ij} c Used	60								
15	Used	65								
20		70				-				
25		75								
30		80								
35		85								
							GNM			
40		90	F	UNCT	TION	KE	Y	FUN	ICTION	KEY
45		95								

NORMAL, INVERSE NORMAL, t AND F DISTRIBUTIONS

These programs evaluate the standard normal density function f(x), the normal integral Q(x) for a given x and the cumulative distribution P(x) for a given x and degrees of freedom v, and the integral of the F distribution for given values of x.

Equations:

1. Standard normal density

$$f(x) = \frac{1}{\sqrt{2\pi}} e^{-\frac{x^2}{2}}$$

2. Normal integral

$$Q = \frac{1}{\sqrt{2\pi}} \int_{x}^{\infty} e^{-\frac{t^2}{2}} dt.$$

(Solving for x given Q as the inverse normal distribution)

3. t density function

$$f(x) = \frac{\Gamma\left(\frac{\nu+1}{2}\right)}{\sqrt{\pi\nu} \Gamma\left(\frac{\nu}{2}\right)} \left(1 + \frac{x^2}{\nu}\right)^{-\frac{\nu+1}{2}}$$

4. Cumulative distribution function

$$P(x) = \int_{-\infty}^{x} f(y) dy$$

5. F distribution

$$P(x) = \int_{x}^{\infty} \frac{\Gamma\left(\frac{\nu_{1} + \nu_{2}}{2}\right) y^{\frac{\nu_{1}}{2} - 1} \left(\frac{\nu_{1}}{\nu_{2}}\right)^{\frac{\nu_{1}}{2}}}{\Gamma\left(\frac{\nu_{1}}{2}\right) \Gamma\left(\frac{\nu_{2}}{2}\right) \left(1 + \frac{\nu_{1}}{\nu_{2}} y\right)^{\frac{\nu_{1} + \nu_{2}}{2}}} dy$$

Reference:

Abramowitz and Stegun, <u>Handbook of Mathematical Functions</u>, National Bureau of Standards, 1970.

```
Example 1: (Program 1)
  Using normal distribution, find f(x) and Q(x) for x = 1.18.
 Keystrokes:
                                                Display:
 [USER]
                                                             (set USER mode)
 [XEQ] [ALPHA] SIZE [ALPHA] 016
 [XEQ] [ALPHA] NORMAL [ALPHA]
                                               0.0000
 1.18 [A]
                                               F=0.1989
                                                            (f(1.18))
 1.18 [B]
                                               Q=0.1190
                                                            (Q(1.18))
 Example 2: (Program 2)
 Using t distribution, find f(x) and P(x) for x = 2.2, v = 11.
 Keystrokes:
                                               Display:
 [USER]
                                                             (set USER mode)
 [XEQ] [ALPHA] SIZE [ALPHA] 013
[XEQ] [ALPHA] T [ALPHA]
                                               0.0000
11 [A]
                                               V=11.0000
2.2 [B]
                                               F=0.0437
                                                           (f(2.2))
2.2 [C]
                                              P=0.9750
                                                           (P(2.2))
Example 3:
            (Program 3)
Using F distribution, find P(x) for x = 4.21, v_1 = 7, v_2 = 6.
Keystrokes:
                                              Display:
[USER]
                                                             (set USER mode)
[XEQ] [ALPHA] SIZE [ALPHA] 008
[XEQ] [ALPHA] FDIST [ALPHA]
                                              0.0000
7 [A]
                                              V1=7.0000
6 [B]
                                              V2=6.0000
4.21 [C]
                                              P=0.0499
                                                           (P(4.21))
```

User Instructions

SIZE: 016

				SIZE: 016	
STEP	INSTRUCTIONS	INPUT	FUNCTION	DISPLAY	
1.	Load program and set USER mode		[USER]		
2.	Initialize		[XEQ] NORMAL	0.0000	
3.	Key in x to compute f(x)	х	[A]	F=	
4.	Key in x to compute Q(x)	x	[B]	Q=.	
5.	Key in Q(x) to compute x	Q(x)	[C]	X=	
6.	For a new case, return to step 3,4, or 5.				
		1 101 101			1
					1
				-	
					1
					1
					1
					-
					1
					4
					+
		1			╛

01+LBL "NOR	Initialize and	46 RTN	
MAL"	store coeffi-	47 "F"	
02 CF 00	cients	48 GTO 09	
03 CF 01		49◆LBL B	
04 CF 02		50 STO 00	
05 SF 21		51 SF 02	Input x to
06 .2316419		52 XEQ A	calculate Q(x)
07 STO 02		53 CF 02	
08 1.330274		54 RCL 00	
429		55 X<0?	
09 STO 03		56 GTO 01	
10 -1.82125		57 SF 00	
5978		58+LBL 13	
11 STO 04		59 1	
12 1.781477 937		60 RCL 00	
13 STO 05		61 RCL 02	
14356563		62 *	1
782		63 + 64 1/X	
15 STO 06		65 ENTERT	
16 .3193815		66 ENTERT	
3		67 ENTERT	i
17 STO 07		68 RCL 03	
18 2.515517		69 *	
19 STO 09		70 RCL 04	
20 .802853		71 +	
21 STO 10		72 *	
22 .010328		73 RCL 05	
23 STO 11		74 +	
24 1.432788		75 *	
25 STO 12		76 RCL 06	
26 .189269		77 +	
27 STO 13		78 *	
28 .001308		79 RCL 07	
29 STO 14 30 CLX		80 +	
30 CLA 31 RTN		81 *	
32+LBL A		82 RCL 01 83 *	
33 STO 00	Input x to	84 "Q"	
34 X12	calculate f(x)	85 FS? 00	
35 2	carcurate I(x)	86 GTO 09	
36 /		87 RTN	
37 CHS		88+LBL 01	
38 E†X		89 CF 00	
39 PI		90 RCL 00	
40 2		91 CHS	
41 *		92 STO 00	
42 SQRT		93 XEQ 13	
43 /		94 1	
44 STO 01		95 X<>Y	
45 FS? 02		96 -	

97 STO 88 98 "Q" 99 GTO 89 100+LBL C 101 X-67 102 GTO 60 103 1 104 X < = Y? 105 GTO 80 106 RDN 107 .5 108 X <> Y 109 X > Y 109 X > Y 110 XEQ 88 111 X 2 111 X 2 112 IX 113 LN 114 SQRT 115 STO 15 116 RCL 11 117 * 118 RCL 10 119 + 120 RCL 15 121 * 122 RCL 89 123 + 124 RCL 15 125 RCL 14 126 * 127 RCL 13 128 + 129 RCL 15 130 * 131 RCL 12 132 + 133 RCL 15 134 * 135 I 136 C + 137 X < Y 138 RCL 15 139 X <> Y 140 - 141 FS? 81 142 CHS 143 GTO 10 144 LBL 88 145 SF 61 146 I 147 -				
98 "Q" 99 GTO 09 100+LBL C 101 X<0? 102 GTO 00 103 1 104 X<=Y? 105 GTO 00 107 .5 108 X<>Y 109 XXY? 109 XXY? 109 XXY? 110 XEQ 08 111 X†2 112 1/X 113 LN 114 SQRT 115 STO 15 116 RCL 11 117 * 118 RCL 10 119 + 120 RCL 15 121 * 122 RCL 09 123 + RCL 15 125 RCL 14 126 RCL 15 127 RCL 13 128 + 129 RCL 15 130 * 131 RCL 15 134 * 132 RCL 15 134 * 135 RCL 15 136 + 137 X	97 STO 08		148 CHS	
99 GTO 09 100+LBL C 101 X(0? 102 GTO 60 103 i 104 X(=??) 105 GTO 00 106 RDN 107 .5 108 X(>Y 109 X)Y? 109 XY? 110 XEQ 08 111 X†2 112 1/X 113 LN 114 SQRT 115 STO 15 116 RCL 11 117 * 118 RCL 10 119 + 120 RCL 15 121 * 122 RCL 09 123 + 124 RCL 15 129 RCL 15 120 RCL 13 128 + 129 RCL 15 130 RCL 15 131 RCL 12 132 X + 133 RCL 15 130 RCL 15 130 RCL 15 131 RCL 12 132 X + 133 RCL 15 130 RCL 15 131 RCL 12 132 X + 133 RCL 15 134 * 135 1 136 + 137 / 138 RCL 15 139 X(>Y 140 - 141 FS? 01 142 CHS 143 GTO 100 144 + LBL 08 145 SF 01 146 1 146 1 150	_		· f	
160 + LBL C 101				Data orror
101 X<0? 102 GTO 00 103 1 104 X<=Y? 105 GTO 00 106 RDN 107 .5 108 X<>Y 110 MEQ 08 111 X12 112 1/X 113 LN 114 SQRT 115 STO 15 116 RCL 11 117 * 118 RCL 10 119 + 120 RCL 15 121 RCL 12 122 RCL 13 128 + 124 RCL 15 125 RCL 14 126 * 127 RCL 13 128 + 129 RCL 15 130 * 131 RCL 12 132 + 133 RCL 15 134 * 135 I 136 + 137 / 138 RCL 15 139 X<>Y 140 - 141 FS? 01 142 CHS 143 GTO 100 144 + LBL 08 144 SF 01 146 1 146 I Input Q(x) to 152 / LB 153 + 154 LBL 10 155 + LB 00 0utput routine Output routine Output routine Output routine Output routine Output routine Output routine		1	•	Data elloi
102 GTO 80 103 1 104 X<=Y? 105 GTO 00 106 RDN 107 .5 108 X<>Y 109 X>Y? 110 XEQ 08 111 X12 112 1/X 113 LN 114 SQRT 115 STO 15 116 RCL 11 117 * 118 RCL 10 119 + 120 RCL 15 121 * 122 RCL 09 123 + 124 RCL 15 125 RCL 14 126 * 127 RCL 13 128 + 129 RCL 15 130 * 131 RCL 15 130 * 131 RCL 15 134 * 137 / 138 RCL 15 139 X<>Y 140 - 141 FS? 01 142 CHS 143 GTO 10 144 + LBL 08 145 SF 01 146 1 Input Q(x) to 153 + LBL 18 154 * "" 155 + LBL 09 156 CF 02 157 CF 01 158 CF 00 159 " +=" 160 ARCL X 161 AVIEW 162 .END. 104 PS 164 PS 164 165 PS 164 167 PS 164 168 PS 164 168 PS 164 175 PS 164 175 PS 164 175 PS 164 175 PS 165 175 PS 165 175 PS 165 175 PS 165 175 PS 167 175 PS 1				
103 1 104 X <= Y? 105 GTO 00 106 RDN 107 .5 108 X <> Y 109 X > Y 1		Input O(x) to		
104 X<=Y? 105 GTO 00 106 RDN 117 .5 118 X<>Y 119 X>Y? 110 XEQ 08 111 X42 112 1/X 113 LN 114 SQRT 115 STO 15 116 RCL 11 117 * 118 RCL 10 119 + 120 RCL 15 121 * 122 RCL 09 123 + 124 RCL 15 125 RCL 14 126 * 127 RCL 13 128 + 129 RCL 15 130 * 131 RCL 12 132 + 133 RCL 15 134 * 135 1 136 + 137 / 138 RCL 15 139 X<>Y 140 — 141 FS? 01 142 CHS 143 GTO 10 144 LBL 08 145 SF 01 146 1 For Q(x) < .5				
105 GTO 00 106 RDN 107 .5 108 X <y *="" +="" -="" .5="" .5<="" 01="" 08="" 09="" 1="" 10="" 11="" 1108="" 1109="" 111="" 112="" 113="" 114="" 115="" 116="" 117="" 118="" 119="" 1197="" 12="" 120="" 121="" 122="" 123="" 124="" 125="" 126="" 127="" 128="" 129="" 13="" 130="" 131="" 132="" 133="" 134="" 135="" 136="" 137="" 138="" 139="" 14="" 140="" 141="" 144="" 145="" 146="" 15="" <="" for="" fs?="" i="" lbl="" ln="" q(x)="" rcl="" sf="" sqrt="" sto="" td="" x="" x<y="" xcy="" xeq="" xt2=""><td></td><td>carcarace x</td><td>1</td><td>Output routine</td></y>		carcarace x	1	Output routine
106 RDN 107 .5 108 X<>Y 109 XY? 1109 XY? 1109 XYP 1109 XYP 1109 ARCL X 111 XT2 111 XT2 112 1/X 113 LN 114 SQRT 115 STO 15 116 RCL 11 117 * 118 RCL 10 119 + 120 RCL 15 121 * 122 RCL 09 123 + 124 RCL 15 125 RCL 14 126 * 127 RCL 13 128 + 129 RCL 15 130 * 131 RCL 12 132 + 133 RCL 15 134 * 135 1 136 + 137 / 138 RCL 15 139 X<>Y 140 - 141 FS? 01 144 LBL 08 145 SF 01 146 1 For Q(x) < .5				'
107 .5 108 X			1	
108 X < Y	I .			1
109 XY? 110 XEQ 08 111 X†2 112 1/X 113 LN 114 SQRT 115 STO 15 116 RCL 11 117 * 118 RCL 10 119 + 120 RCL 15 121 * 122 RCL 09 123 + 124 RCL 15 125 RCL 14 126 * 127 RCL 13 128 + 129 RCL 15 130 * 131 RCL 12 132 + 133 RCL 15 134 * 135 1 136 + 137 / 138 RCL 15 137 X 138 RCL 15 139 X <y -="" 01="" 08="" 10="" 140="" 141="" 142="" 143="" 144+lbl="" 145="" 146="" 1<="" chs="" fs?="" gto="" sf="" td=""><td>_</td><td>-</td><td></td><td> </td></y>	_	-		
110 XEQ 08 111 X72 111 X72 112 1/X 113 LN 114 SQRT 115 STO 15 116 RCL 11 117 * 118 RCL 10 119 + 120 RCL 15 121 * 122 RCL 09 123 + 124 RCL 15 125 RCL 14 126 * 127 RCL 13 128 + 129 RCL 15 130 * 131 RCL 12 132 + 133 RCL 15 134 * 135 1 136 + 137 / 138 RCL 15 139 X<>Y 140 - 141 FS? 01 142 CHS 143 GTO 10 144 LBL 08 145 SF 01 146 1		•		
111 X72 112 1/X 113 LN 114 SQRT 115 STO 15 116 RCL 11 117 * 118 RCL 10 119 + 120 RCL 15 121 * 122 RCL 09 123 + 124 RCL 15 125 RCL 14 126 * 127 RCL 13 128 + 129 RCL 15 130 * 131 RCL 12 132 + 133 RCL 15 134 * 135 1 136 + 137 / 138 RCL 15 137 / 138 RCL 15 139 X <y -="" .5<="" 01="" 08="" 1="" 10="" 140="" 141="" 142="" 143="" 144+lbl="" 145="" 146="" <="" chs="" for="" fs?="" gto="" q(x)="" sf="" td=""><td></td><td></td><td></td><td></td></y>				
112 1/X 113 LN 114 SQRT 115 STO 15 116 RCL 11 117 * 118 RCL 10 119 + 120 RCL 15 121 * 122 RCL 09 123 + 124 RCL 15 125 RCL 14 126 * 127 RCL 13 128 + 129 RCL 15 130 * 131 RCL 12 132 + 131 RCL 12 132 + 133 RCL 15 134 * 135 1 136 + 137 / 138 RCL 15 139 X<>Y 140 - 141 FS? 01 142 CHS 143 GTO 10 144+LBL 08 145 SF 01 146 1				
113 LN 114 SQRT 115 ST0 15 116 RCL 11 117 * 118 RCL 10 119 + 120 RCL 15 121 * 122 RCL 09 123 + 124 RCL 15 125 RCL 14 126 * 127 RCL 13 128 + 129 RCL 15 130 * 131 RCL 12 132 + 133 RCL 15 134 * 135 1 136 + 137 / 138 RCL 15 139 X<>Y 140 - 141 FS? 01 142 CHS 143 GTO 10 144 LBL 08 145 SF 01 146 1	_ = ::	1	102 12:10:	
114 SQRT 115 STU 15 116 RCL 11 117 * 118 RCL 10 119 + 120 RCL 15 121 * 122 RCL 09 123 + 124 RCL 15 125 RCL 14 126 * 127 RCL 13 128 + 129 RCL 15 130 * 131 RCL 12 132 + 133 RCL 15 134 * 135 1 136 + 137 / 138 RCL 15 139 X<>Y 140 - 141 FS? 01 142 CHS 143 GTO 10 144 LBL 08 145 SF 01 146 1				
115 STO 15 116 RCL 11 117 * 118 RCL 10 119 + 120 RCL 15 121 * 122 RCL 09 123 + 124 RCL 15 125 RCL 14 126 * 127 RCL 13 128 + 129 RCL 15 130 * 131 RCL 12 132 + 133 RCL 15 134 * 135 1 136 + 137 / 138 RCL 15 139 X<>Y 140 - 141 FS? 01 142 CHS 143 GTO 10 144+LBL 08 145 SF 01 146 1	· ·]
116 RCL 11 117 * 118 RCL 10 119 + 120 RCL 15 121 * 122 RCL 09 123 + 124 RCL 15 125 RCL 14 126 * 127 RCL 13 128 + 129 RCL 15 130 * 131 RCL 12 132 + 133 RCL 15 134 * 135 1 136 + 137 / 138 RCL 15 139 X<>Y 140 - 141 FS? 01 142 CHS 143 GTO 10 144+LBL 08 145 SF 01 146 1]		
117 * 118 RCL 10 119 + 120 RCL 15 121 * 122 RCL 09 123 + 124 RCL 15 125 RCL 14 126 * 127 RCL 13 128 + 129 RCL 15 130 * 131 RCL 12 132 + 133 RCL 15 134 * 135 1 136 + 137 / 138 RCL 15 139 X<> 131 RCL 15 134 * 135 1 136 + 137 / 138 RCL 15 139 X<> 140 - 141 FS? 01 142 CHS 143 GTO 10 144+LBL 08 145 SF 01 146 1				
118 RCL 10 119 + 120 RCL 15 121 * 122 RCL 09 123 + 124 RCL 15 125 RCL 14 126 * 127 RCL 13 128 + 129 RCL 15 130 * 131 RCL 12 132 + 133 RCL 15 134 * 135 1 136 + 137 / 138 RCL 15 139 X<>Y 140 - 141 FS? 01 142 CHS 143 GTO 10 144+LBL 08 145 SF 01 146 1	•]	70	
119 + 120 RCL 15 121 * 122 RCL 09 123 + 124 RCL 15 125 RCL 14 126 * 127 RCL 13 128 + 129 RCL 15 130 * 131 RCL 12 132 + 133 RCL 15 134 * 135 1 136 + 137 / 138 RCL 15 139 X<>Y 140 - 141 FS? 01 142 CHS 143 GTO 10 144+LBL 08 145 SF 01 146 1	_			
120 RCL 15 121 * 122 RCL 09 123 + 124 RCL 15 125 RCL 14 126 * 127 RCL 13 128 + 129 RCL 15 130 * 131 RCL 12 132 + 133 RCL 15 134 * 135 1 136 + 137 / 138 RCL 15 139 X<>Y 131 RCL 15 139 X<>Y 140 - 141 FS? 01 142 CHS 143 GTO 10 144+LBL 08 145 SF 01 146 1				1
121 * 122 RCL 09 123 + 124 RCL 15 125 RCL 14 126 * 127 RCL 13 128 + 129 RCL 15 130 * 131 RCL 12 132 + 133 RCL 15 134 * 135 1 136 + 137 / 138 RCL 15 139 X<>Y 140 - 141 FS? 01 142 CHS 143 GTO 10 144+LBL 08 145 SF 01 146 1 For Q(x) < .5				
122 RCL 09 123 + 124 RCL 15 125 RCL 14 126 * 127 RCL 13 128 + 129 RCL 15 130 * 131 RCL 12 132 + 133 RCL 15 134 * 135 1 136 + 137 / 138 RCL 15 139 X<>Y 140 - 141 FS? 01 142 CHS 143 GTO 10 144 LBL 08 145 SF 01 146 1	i e	1		1
123 + 124 RCL 15 125 RCL 14 126 * 127 RCL 13 128 + 129 RCL 15 130 * 131 RCL 12 132 + 133 RCL 15 134 * 135 1 136 + 137 / 138 RCL 15 139 X<>Y 140 - 141 FS? 01 142 CH8 143 GTO 10 144 LBL 08 145 SF 01 146 1		1		1
124 RCL 15 125 RCL 14 126 * 127 RCL 13 128 + 129 RCL 15 130 * 131 RCL 12 132 + 133 RCL 15 134 * 135 1 136 + 137 / 138 RCL 15 139 X<>Y 140 - 141 FS? 01 142 CHS 143 GTO 10 144+LBL 08 145 SF 01 146 1	,			1
125 RCL 14 126 * 127 RCL 13 128 + 129 RCL 15 130 * 131 RCL 12 132 + 133 RCL 15 134 * 135 1 136 + 137 / 138 RCL 15 139 X<>Y 140 - 141 FS? 01 142 CHS 143 GTO 10 144+LBL 08 145 SF 01 146 1				
126 * 127 RCL 13 128 + 129 RCL 15 130 * 131 RCL 12 132 + 133 RCL 15 134 * 135 1 136 + 137 / 138 RCL 15 139 X<>Y 140 - 141 FS? 01 142 CHS 143 GTO 10 144 LBL 08 145 SF 01 146 1 For Q(x) < .5		1		
127 RCL 13 128 + 129 RCL 15 130 * 131 RCL 12 132 + 133 RCL 15 134 * 135 1 136 + 137 / 138 RCL 15 139 X<>Y 140 - 141 FS? 01 142 CHS 143 GTO 10 144 LBL 08 145 SF 01 146 1 For Q(x) < .5	1	•		1
127 RCL 13 128 + 129 RCL 15 130 * 131 RCL 12 132 + 133 RCL 15 134 * 135 1 136 + 137 / 138 RCL 15 139 X<>Y 140 - 141 FS? 01 142 CHS 143 GTO 10 144 LBL 08 145 SF 01 146 1 For Q(x) < .5		1	80	1
129 RCL 15 130 * 131 RCL 12 132 + 133 RCL 15 134 * 135 1 136 + 137 / 138 RCL 15 139 X<>Y 140 - 141 FS? 01 142 CHS 143 GTO 10 144+LBL 08 145 SF 01 146 1 For Q(x) < .5		†		1 1
130 * 131 RCL 12 132 + 133 RCL 15 134 * 135 1 136 + 137 / 138 RCL 15 139 X<>Y 140 - 141 FS? 01 142 CHS 143 GTO 10 144+LBL 08 145 SF 01 146 1 For Q(x) < .5		1		1
131 RCL 12 132 + 133 RCL 15 134 * 135 1 136 + 137 / 138 RCL 15 139 X<>Y 140 - 141 FS? 01 142 CHS 143 GTO 10 144+LBL 08 145 SF 01 146 1 For Q(x) < .5	_ ::	1		†
131 RCL 12 132 + 133 RCL 15 134 * 135 1 136 + 137 / 138 RCL 15 139 X<>Y 140 - 141 FS? 01 142 CHS 143 GTO 10 144 LBL 08 145 SF 01 146 1 For Q(x) < .5		1		1 ,
133 RCL 15 134 * 135 1 136 + 137 / 138 RCL 15 139 X<>Y 140 - 141 FS? 01 142 CHS 143 GTO 10 144+LBL 08 145 SF 01 146 1 For Q(x) < .5	· ·	1		
134 * 135 1 136 + 137 / 138 RCL 15 139 X<>Y 140 - 141 FS? 01 142 CHS 143 GTO 10 144+LBL 08 145 SF 01 146 1 For Q(x) < .5		•		- I
135 1 136 + 137 / 138 RCL 15 139 X<>Y 140 - 141 FS? 01 142 CHS 143 GTO 10 144+LBL 08 145 SF 01 146 1 For Q(x) < .5		1		
136 + 137 / 138 RCL 15 139 X<>Y 140 - 141 FS? 01 142 CHS 143 GTO 10 144+LBL 08 145 SF 01 146 1 For Q(x) < .5				
137 / 138 RCL 15 139 X<>Y 140 - 141 FS? 01 142 CHS 143 GTO 10 144+LBL 08 145 SF 01 146 1				4
138 RCL 15 139 X<>Y 140 - 141 FS? 01 142 CHS 143 GTO 10 144+LBL 08 145 SF 01 146 1 For Q(x) < .5			L 00	
139 X<>Y 140 - 141 FS? 01 142 CHS 143 GTO 10 144+LBL 08 145 SF 01 146 1			90	
140 - 141 FS? 01 142 CHS 143 GTO 10 144+LBL 08 145 SF 01 146 1 For Q(x) < .5				4
141 FS? 01 142 CHS 143 GTO 10 144+LBL 08 145 SF 01 146 1	_			
142 CHS 143 GTO 10 144+LBL 08 145 SF 01 146 1]
143 GTO 10 144+LBL 08 145 SF 01 146 1	l			
144+LBL 08 145 SF 01 146 1	_]
145 SF 01 146 1 For Q(x) < .5]
146 1]
146 1		$\int For O(x) < .5$		_
147 - 00				
	147 -		00	

REGISTERS, STATUS, FLAGS, ASSIGNMENTS 25

	D	ATA REGISTERS	STATUS
00	x f(x) r b ₅	50	SIZE
05	b 4 b 3	55	INIT
	b ₂		# S/C SET INDICATES CLEAR INDICATES
<u> </u>	b _l USED		00 Positive
ļ	C ₀		$\begin{array}{c ccccccccccccccccccccccccccccccccccc$
10	C ₁	60	
	C ₂	- 00	21 Printer enable
	d_1		
	d ₂		
	d ₃		
15	t	65	
ļ			
20		70	
20		70	
25		75	
30		80	
35		85	
-55	· · · · · · · · · · · · · · · · · · ·		
			ASSIGNMENTS
			FUNCTION KEY FUNCTION KEY
40		90	
45		05	
45		95	

User Instructions

SIZE: 013 **INPUT FUNCTION** DISPLAY STEP **INSTRUCTIONS** Load program and set USER mode [USER] Initialize [XEQ] T 0.0000 Key in degrees of freedom $\boldsymbol{\nu}$ 3. [A] 4. Key in x to compute f(x)F= [B] 5. Key in x to compute P(x)P≖ [C] For a new case with the same ν , go to step 4 or 5. For a new case with a different ν , go to step 3.

	•		
01+LBL "T"	Initialize	52 INT	
02 SF 21		53 LASTX	
03 CF 01		54 X≠Y?	
04 CLX		55 GTO 01	
05 RTN		56 1	
, 06+LBL A	- ·	57 -	
07 STO 00 08 "V"	Input v	58 FACT	
08 "V" 09 GTO 10		59 STO 03	
10+LBL B		60 RTN	
11 STO 12	+	61+LBL 01	Check for
12 RCL 00		62 .5 63 X=Y?	v/2 = 1/2
13 XEQ 11	Input ha	64 GTO 02	
14 STO 10	Input x to calculate f(x)	65 X<>Y	
15 RCL 00	carculate 1(x)	66 1	
16 1		67 -	
17 +		68 ST* 03	
18 XEQ 11		69 GTO 01	
19 STO 09		70+LBL 02	
20 RCL 12		71 PI	$\Gamma(\frac{1}{2})$
21 RCL 09.		72 SQRT	1 (2)
22 RCL 10		73 RCL 03	ı
23 /		74 *	
24 PI		75 STO 03	
25 RCL 00		76 RTN	
26 * 27 SQRT		77+LBL C	
27 39K1		78 STO 12	
29 1		79 ABS	Input x to
30 RCL 12		80 RCL 00 81 RAD	calculate P(x)
31 X†2		82 SQRT	
32 RCL 00		83 /	
33 /		84 ATAN	:
34 +		85 STO 02	i
35 RCL 00		86 RCL 00	
36 1		87 2	
37 +		88 /	
38 2		89 INT	
39 /		90 LASTX	
40 CHS		91 X≠Y?	!
41 YTX		92 GTO 04	
42 * 43 "F"		93 0	
l		94 STO 05	į
44 GTO 10 45+LBL 11		95+LBL 12	
46 1	Calculate P(v/2)	96 RCL 02	
47 STO 03	Calculate Γ(ν/2)	97 COS 98 X↑2	
48 X<>Y		98 ATZ 99 STO 03	
49 2	1	100 RCL 02	
50 /		100 KCL 02 101 SIN	
51 STO 01		102 STO 04	

103 RCL 00 104 2 105 X=Y? 106 GTO 08 107 / 108 INT 109 STO 11 110 1 111 STO 06 112 DSE 11 113 GTO 03 114 GTO 13 115 LBL 03 116 RCL 03		154 COS 155 * 156 2 157 * 158 PI 159 / 160 RCL 07 161 + 162 RCL 12 163 GTO 06 164+LBL 09 165 RCL 07 166 RCL 12 167 GTO 06	For odd v
117 * 118 RCL 05 119 1 120 + 121 * 122 LASTX	For even v	168+LBL 08 169 RCL 04 170 RCL 12 171+LBL 06 172 X>0? 173 GTO 00	For even v Calculate P(x) from R(x)
123 1 124 + 125 STO 05 126 / 127 ST+ 06 128 DSE 11 129 GTO 03		174 X<>Y 175 1 176 - 177 CHS 178 2 179 / 180 "P"	for x < 0
130 RCL 06 131+LBL 13 132 RCL 04 133 * 134 FS? 01 135 RTN 136 RCL 12 137 GTO 06 138+LBL 04		181 GTO 10 182+LBL 00 183 X<>Y 184 1 185 + 186 2 187 / 188 "P" 189+LBL 10	Calculate P(x) for x > 0
139 RCL 02 140 2 141 * 142 PI 143 / 144 STO 07 145 RCL 00 146 1	For odd v	190 "F=" 191 ARCL X 192 AVIEW 193 .END.	Output routine
147 STO 05 148 X=Y? 149 GTO 09 150 SF 01 151 XEQ 12 152 CF 01 153 RCL 02		00	

REGISTERS, STATUS, FLAGS, ASSIGNMENTS

DATA REGISTERS			STATUS
00	∪ USED ⊖ USED	50	SIZE SIZE TOT. REG 47 USER MODE ENG FIX SCI ON OFF DEG RAD GRAD
05	SIN 0 USED USED	55	FLAGS INIT # S/C SET INDICATES CLEAR INDICATES
	2Θ/π, R USED		01 odd v
10	Γ (ν+1/2) Γ (ν/2) Index	60	21 Printer enable
	х		
15		65	
20		70	
25		75	
30		80	
35		85	
			ASSIGNMENTS
40		90	FUNCTION KEY FUNCTION KEY
45		95	

User Instructions

SIZE: 008

				0.22. 000	_
STEP	INSTRUCTIONS	INPUT	FUNCTION	DISPLAY	
1.	Load program and set USER mode.		[USER]		
2.	Initialize		[XEQ] FDIST	0.0000	
3.	Key in v_1	ν1	[A]	v1=	
4.	Key in v_2	ν ₂	[B]	V2 =	
5.	Key in x to calculate P(x)		[C]	P =	
6.	For a new case to to step 3.				
					-
					1
					1
					1
					1
					1
					-
					1
					7
					-
					\dashv
					\dashv
				-	\dashv
					-
					-

01+LBL "FDI	Initialize	51 1	
ST"	IIIICIAIIZE	52 STO 05	
02 SF 21	1	53 RCL 03	
03 CF 01	1	54 -	
04 0	İ	55 STO 03	
05 STO 05	İ	56 RCL 02	
Ø6 RTN	•	57 2	
07◆LBL A	1	58 /	
Ø8 STO Ø1	Input V ₁	59 *	
09 "V1"	Impac VI	60 ST+ 05	į
10 GTO 10		61 DSE 00	
11+LBL B		62 GTO 03	İ
12 STO 02	Input v_2	63 GTO 02	
13 "V2"	-	64+LBL 03	
14 GTO 10	İ	65 RCL 02	1
15+LBL C		66 2	
16 "P"		67 +	
17 STO 06			
18 RCL 01	1	68 STO 02	
19 *]	69 RCL 07	•
20 RCL 02		70 2	
20 KCL 02		71 +	
22 LASTX		72 STO 07	•
23 X<>Y		73 /	
24 /		74 RCL 03	
25 STO 03		75 *	
r	If v_1 odd then	76 *	
26 RCL 01 27 2	go to LBL 01	77 ST+ 05	
28 /		78 DSE 00	
		79 GTO 03	
29 FRC		80+LBL 02	
30 X≠0?		81 RCL 05	· ·
31 GTO 01		82 RCL 04	
32+LBL 00	.,	83 *	
33 RCL 03	ν ₁ even	84 RTN	
34 RCL 02		85+LBL 01	
35 2 36 070 07		86 RCL 01	ν ₁ odd
3 <u>6</u> STO 07		87 X<> 02	
37 /		88 STO 01	
38 Y1X		89 1	
39 STO 04		90 RCL 03	
40 RCL 01		91 -	
41 2		92 STO 03	
42 -		93 XEQ 00	
43 2		94 1	
44 /		95 X<>Y	
45 STO 00		96 -	
46 X≠0?		97 + LBL 10	Output routine
47 GTO 05		98 "H="	, Jacpar routine
48 RCL 04		99 ARCL X	
49 GTO 10		100 AVIEW	
50+LBL 05		101 .EHD.	
·			<u> </u>

REGISTERS, STATUS, FLAGS, ASSIGNMENTS

DATA REGISTERS				STATUS					
00	USED v_1 or v_2 v_2 or v_1 t, 1-t	50	SIZ ENC DEC	E G	TOT FIX -	. REG28 SCI _ GRAI	USER MO ON X O	DE DFF	
05	USED USED x	55		FLAGS INIT # S/C SET INDICATES			CLEAR IND	CLEAR INDICATES	
	USED		21		Printe	er enable			
10		60							
15		65							
20		70							
25		75							
30		80							
35		85				ASSIGNI	MENTS		
				ASSIGNMENTS FUNCTION KEY FUNCTION KEY				KEY	
40		, 90							
45		95							

BASIC STATISTICS FOR TWO VARIABLES

This program calculates means, standard deviations, covariance, correlation coefficient, and coefficients of variation from ungrouped data points $[(x_i,y_i), i=1,2,...,n]$ or grouped data points $[(x_i,y_i,f_i), i=1,2,...,n]$. f_i denotes the frequency of repetition of (x_i,y_i) .

Equations:

Mean

$$\overline{x} = \frac{1}{n} \sum_{i=1}^{n} x_i$$

$$\overline{y} = \frac{1}{n} \sum_{i=1}^{n} y_i$$

Standard deviation

$$s_{x} = \sqrt{\frac{\sum x_{i}^{2} - n\overline{x}^{2}}{n-1}}$$

$$s_{x} = \sqrt{\frac{\sum x_{i}^{2} - n\overline{x}^{2}}{n}}$$

$$s_{y} = \sqrt{\frac{\sum y_{i}^{2} - n\overline{y}^{2}}{n-1}}$$

$$s_{y} = \sqrt{\frac{\sum y_{i}^{2} - n\overline{y}^{2}}{n}}$$

covariance

$$s_{xy} = \frac{1}{n-1} \left(\sum x_i y_i - \frac{1}{n} \sum x_i y_i \right)$$

$$s_{xy}' = \frac{1}{n} \left(\sum x_i y_i - \frac{1}{n} \sum x_i y_i \right)$$

correlation coefficient

$$\gamma_{xy} = \frac{s_{xy}}{s_x s_y}$$

coefficients of variation

$$V_{x} = \frac{s_{x}}{\overline{x}}$$
 .100, $V_{y} = \frac{s_{y}}{\overline{y}}$.100

Note: n is a positive integer > 1.

Example:

For the following set of data, find the means, standard deviations, covariance, correlation coefficient and coefficients of variation.

x.	4.8	5.2	4.1	3.8
y_{i}	15.1	11.5	13.6	14.3
fi	1	3	2	1

Keystrokes:	Display:
[USER]	(set USER mode)
[XEQ] [ALPHA] SIZE [ALPHA] 017	
[XEQ] [ALPHA] STAT [ALPHA]	0.0000
4.8 [ENTER†] 15.1 [ENTER†] 1 [B]	1.0000
5.2 [ENTER†] 11.5 [ENTER†] 3 [B]	4.0000
4.1 [ENTER†] 13.6 [ENTER†] 2 [B]	6.0000
3.8 [ENTER†] 14.3 [ENTER†] 1 [B]	7.0000
[C]	MEANX=4.6286
[R/S]	MEANY=13.0143
[R/S]	VX=13.2429
[R/S]	VY=11.5550
[D]	SX=0.6130
[R/S]	SY=1.5038
[R/S]	SX.=0.5675
[R/S]	SY.=1.3923
[E]	SXY = -0.6538
[R/S]	SXY. = -0.5604
[R/S]	VXY = -0.7093

				SIZE: 017
STEP	INSTRUCTIONS	INPUT	FUNCTION	DISPLAY
1.	Load program and set USER mode		[USER]	
2.	Initialize		[XEQ] STAT	0.0000
3.	For grouped data points, go to step 6.			
	For ungrouped data points, go to			
-	step 4.			
4.	For $i = 1, 2, \ldots, n$, key in x_i and y_i	x _i	[ENTER ↑]	
		y _i	[A]	i
5.	If you made a mistake in keying in x			
	and y, the correct by	x k	[ENTER †]	
		y _k	[///] [A]	i-l
6.	For i = 1, 2,, n, key in x, y and			
	f (grouped data)	×	[ENTER 1]	
		y _i	[ENTER ↑]	
		f	[B]	fi
7.	If you made a mistake in keying in x, y			
	and f, then correct by	x k	[ENTER 1]	
		y _k	[ENTER 1]	
	_	f_k	[///] [B]	f _i - f _k
	Calculate means (x and y) and coefficients			
	of variation (V and V y)		[C]	MEANX =
			[R/S]	MEANY =
			[R/S]	ΛX =
			[R/S]	VY =
	Calculate standard deviations			
	(s, s, s and s ')		[D]	SX =
			[R/S]	SY =
			[R/S]	SX. =

				SIZE: 017
STEP	INSTRUCTIONS	INPUT	FUNCTION	DISPLAY
			[R/S]	SY.=
10.	Calculate covariance and correlation			
	coefficient (s _{xy} , s _{xy} ', and V _{xy})		[E]	SXY=
	ny ny		[R/S]	SXY.=
			[R/S]	VXY=
11.	For a new case, go to step 2.			
:				

		-		
			-	

01+LBL "STA	Todadalda	51+LBL C	
7 "	Initialize	52 MEAN	
02 CLRG		53 STO 00	Calculate x, y,
03 SF 21		54 "MEANX="	
04 CF 00		55 XEQ 00	V_{x}, V_{y}
05 CF 01		56 X<>Y	
06 CLX		57 STO 02	
07 RTN		58 "MEANY="	
08◆LBL a	Correction for	59 XEQ 00	
09 X<>Y	x _k ,y _k	60 SDEV	
10 Σ-	K K	61 1 E2	İ
11 RTN	Ì	62 *	1
12+LBL A		63 X<>Y	
13 X<>Y	Input x,y	64 LASTX	
14 Σ+	1 1 1	65 *	
15 RTN		66 X<>Y	
16+LBL B 17 STO 05		67 RCL 00	
17 510 03 18 FS? 01	Input x _i ,y _i ,f _i	68 /	
19 CHS	1 1 1	69 "VX="	
20 ST+ 01		70 XEQ 00	
21 RDN		71 X<>Y	
22 STO 04		72 RCL 02	
23 RDN		73 / 74 "VY="	
24 STO 03		75 XEQ 00	
25 R↑		75 AEW 99	
26 R1		77 + LBL D	
27 ABS		78 SDEV	Calculate S _x ,S _y ,
28 STO 06]	79 "SX="	$\begin{bmatrix} s_x', s_y' \end{bmatrix}$
29+LBL 02		80 XEQ 00	х у
30 RCL 04		81 X<>Y	
31 RCL 03		82 "SÝ="	
32 XEQ 03		83 XEQ 00	
33 DSE 06		84 X<>Y	
34 GTO 02		85+LBL 01	
35 RCL 01		86 RCL 16	
36 STO 16		87 ENTERT	
37 RTH		88 X<>Y	
38◆LBL b		89 i	
39 SF 01	Correction for	90 -	
40 XEQ B	x _k ,y _k ,f _k	91 /	
41 CF 01	R R R	92 SQRT	
42 RTN		93 /	
43+LBL 03		94 FS?C 00	
44 FS? 01		95 GTO 05	
45 GTO 04		96 "SX.="	
46 Σ+ 47 RTN		97 XEQ 00	
47 KIN 48+LBL 04		98 LASTX	
49 Z-		99 SDEV	
50 RTN		100 X<>Y	
OO KIII		101 SF 00	

102 GTO 01		51			
102 G10 91					1
104 "SY.="					1
105 GTO 00					l
106+LBL E	Calculate				l
107 MEAN	S _{xy} , S _{xy}				l
108 X<>Y	xy'xy				ļ
109 STO 02					ĺ
110 RCL 15					l
111 RCL 11		60			1
112 RCL 02					ĺ
113 *					ĺ
114 -					l
115 RCL 16					l
116 1					l
117 -					l
118 / 119 STO 07					
120 "SXY="					
121 XEQ 00					
122 RCL 16		70			
123 ENTERT					
124 X<>Y					
125 1					ĺ
126 -		-			New York
127 /					
128 /					
129 "SXY.="					
130 XEQ 00					
131 SDEV		80			
132 RCL 07					
133 / 134 *					
134 * 135 1/X					
135 17 N 136 "VXY="					
137+LBL 00					
138 ARCL X	Output routine				
139 AVIEW					
140 .END.					
40		90			
		-			
		<u></u>			
		 			
		<u> </u>			
		-	· · · · · · · · · · · · · · · · · · ·		
		-			
		-			
50		00			A a
30	<u> </u>	1 00	<u></u>	<u> </u>	1

REGISTERS, STATUS, FLAGS, ASSIGNMENTS³⁹

	D	ATA REGISTERS	STATUS
00	Σfi y x,	50	SIZE TOT. REG USER MODE ENG FIX SCI ON OFF DEG RAD GRAD
05	x. i y. f,	55	INIT FLAGS
	USED USED		# S/C SET INDICATES CLEAR INDICATES
			01 Correction
10		60	21 Printer enable
	Σχ.		
	Σx Σx ⁱ ² Σy _i Σy _i ² Σx ⁱ y _i		
	$\frac{\Sigma y_{i_2}}{\Sigma y_{i_2}}$		
15	$\Sigma x_{i}^{1}y_{i}$	65	
	n		
20		70	
-20		70	
25		75	
_			
~			
30		80	
35		85	
			ASSIGNMENTS
			FUNCTION KEY FUNCTION KEY
40		90	
45		95	

MOVING AVERAGE

In a moving average, a specified number of data points are averaged. When there is a new piece of input data, the oldest piece of data is discarded to make room for the latest input. This replacement scheme makes the moving average a valuable tool in following trends. The fewer the number of data points, the more trend sensitive the average becomes. With a large number of data points, the average behaves more like a regular average, responding slowly to new input data.

This program allows for a moving average of 14 points with no memory modules and 64 more points with each additional memory module. It also allows for more than one moving average to be computed with the same set of data. For example, instead of obtaining only a 6 month moving average, you could obtain a 3 month and 12 month as well with the same data. For each additional moving average you wish to compute, the maximum number of data points is reduced by three. For example if you have no memory modules and wish to compute 2 moving averages with the same data, the maximum size for an average is 11.

This program is most useful when a card reader is available. With data card(s) to remember your old data points you need only input the most recent data point to compute current moving average(s).

Example 1:

A six period and three period moving average is desired to project monthly sales. The first 6 months of sales follows:

Month	1	2	3	4	5	6
Sales	125	183	207	222	198	240

Compute the 3 month moving average for months 3,4,5, and 6, and the 6 month moving average for month 6.

Keystrokes:	Display:
[XEQ] [ALPHA] SIZE [ALPHA] 006	
[XEQ] [ALPHA] AVG [ALPHA]	NO. OF AVGS ?
2 [R/S]	N MAX?
6 [R/S]	SET SIZE 15 (mark a data card SIZE 015)
[XEQ] [ALPHA] SIZE [ALPHA] 015 [R/S]	N2?
3 [R/S]	DATA ?
125 [R/S]	DATA ?
183 [R/S]	DATA ?
207 [R/S]	DATA ?
[R/S]	MA3=171.6667
[R/S] [R/S]	DATA ?
222 [R/S]	DATA ?
[R/S]	MA3=204.0000
[R/S] [R/S]	DATA ?
198 [R/S]	DATA ?
[R/S]	MA3=209.0000
[R/S] [R/S]	DATA ?
240 [R/S]	DATA ?
[R/S]	MA3=220.0000

Now record the data for example 2.

[XEQ] [ALPHA] UPDATE [ALPHA] RDY 01 OF 01 Insert one side of the data card into the card reader.

Now turn the calculator off assume a month has passed. Turn the calculator on and load the program.

MA6=195.8333

Example 2:

[R/S]

The actual sales for the seventh month totaled 225 units. Compute new moving averages and output the current points in the averages.

Keystrokes:	Display
[XEQ] [ALPHA] SIZE [ALPHA] 015	(as marked on the data card)
load the data card	
[XEQ] [ALPHA] PT [ALPHA]	DATA ?
225 [R/S]	DATA ?
[R/S]	MA3=221.0000
[R/S]	MA6=212.5000
[XEQ] [ALPHA] OUT [ALPHA]	PT1=225.0000
[R/S]	PT2=240.0000
[R/S]	PT3=198.0000
[R/S]	PT4=222.0000
[R/S]	PT5=207.0000
[R/S]	PT6=183.0000

				SIZE: 6+
STEP	INSTRUCTIONS	INPUT	FUNCTION	DISPLAY
1.	Load program.			
2.	If starting new moving average(s) go to			
	step 4.			
3.	Set size to that marked on the data card(s)			
-	(during step 7) containing previous moving			
	average(s) data load the card(s) and go			
	to step 11.		[XEQ] SIZE nnn	
4.	Initialize		[XEQ] AVG	NO. OF AVGS ?
5.	Key in the number of moving averages you			
	wish to compute with the one set of data.	k	[R/S]	N MAX?
6.	Key in the number of points that the			
	longest moving average will deal with.	n max	[R/S]	SET SIZE nnn
7.	Set the required size and mark your data			
	cards with the size (for step 3.)		[XEQ] SIZE nnn	
			[R/S]	N2?(or)DATA?
8.	Key in the length of the other moving			
	averages as they are asked for. When			
	"DATA?" is displayed continue to step 9.	n i	[R/S]	N(i+1)?orDATA?
9.	Key in data as desired. When all the			
	points desired are in, go to step ll or			
	press [R/S] and continue to step 10.	data	[R/S]	DATA ?
			or	
			[R/S]	MA(i)=
10.	Obtain the other moving averages by			
-	pressing [R/S] for each. When one more			
	[R/S] is pressed than is needed you are			
	back to the data input routine,			

SIZE: 6+ **FUNCTION** DISPLAY STEP **INPUT INSTRUCTIONS** [R/S]MA(i) =go to step 9. (or) DATA ? Any of the following steps can be done in 11. any order and at any time after step 8. 12. To input more data: [XEQ]PT DATA ? then go to step 9. 13. To output data in newest to oldest format: [XEQ] OUT PT1 =[R/S] PT2 =[XEQ]AVGS MA(i) =14. To obtain current moving averages: then go to step 10. [XEQ]UPDATE RDY () OF () 15. To store current data on cards: then load cards requested

			
01+LBL "AVG	Initialization	47 RDN	
**		48 1	
02 CLRG		49 +	
03 "NO. OF	1	50+LBL 04	
AVGS ?"	1	51 ISG 02	
04 PROMPT	1	52 GTO 03	†
05 1	•	53+LBL "PT"	Input a data
Ø6 +	1	54 CF 22	point
07 STO 00		55 "DATA ?"	1.
0 8 3	1	56 PROMPT	
09 *		57 RCL 01	1
10 STO 01	1	58 FC?C 22	
11 "N MAX?"	1 n	59 GTO "AVG	If no noint
12 PROMPT	nmax	S"	If no point
13 STO 05	1	IT .	calculate average
14 RCL 01	ļ		
15 +		61 /	
16 FIX 0	ļ	62 4.00003	
17 CF 29		63 +	
		64 STO 02	
		65 1	
_ _	į	66 -	
19 ARCL X		67 X<>Y	
20 PROMPT	Prompt for	68+LBL 01	
21 RCL 00	correct size	69 ST+ IND	Add pt. to Σ's
22 3	İ	Υ	
23 *		70 RCL IND	
24 .96		02	
25 -		71 RCL 05	
26 1 E3		72 MOD	
27 /	·	73 RCL 01	
28 4		74 +	}
29 +		75 RCL IND	
30 STO 02		×]
31 2		76 ST- IND	Subtract ald
32 GTO 04		T	Subtract old pt.
33+LBL 03		77 ISG IND	
34 "N"		02	1
35 ARCL X		78 + LBL 00	Point to next
36 "⊦?"		79 RDN	oldest pt.
37 CF 22		80 RDN	1
38 PROMPT	n	81 ISG Y	1
39 FC?C 22	n i	82 ISG 02	
40 GTO "PT"		83 GTO 01	
41 STO IND		84 RCL 04	
02		85 1	
42 CHS		86 -	
43 1		87 RCL 05	
44 ST- 02			1
45 RDN			
46 STO IND	Pointer:		
92 310 IND	TOTHECT.	90 +	
		91 X<>Y	

92 STO IND Y 93 GTO "PT" 94*LBL "AVG S" 95 CF 29 96 RCL 01 97 3 98 - 99 .00205	Compute the moving averages	137 FIX 0 138 ARCL 02 139 "F=" 140 FIX 4 141 ARCL IND X 142 PROMPT 143 RDN 144 ISG 02 145 GTO 05 146 GTO "OUT	Output point
101 STO 02 102+LBL 02 103 RCL IND 02 104 2 105 ST+ 02 106 RDN 107 RCL IND 02 108 / 109 "MA" 110 FIX 0	Store counter Recall Σ i Recall n i	" 147+LBL "UPD ATE" 148 WDTA 149 RTN 150 .END.	Update data card(s)
111 ARCL IND 02 112 "F=" 113 FIX 4 114 ARCL X 115 PROMPT 116 DSE 02 117 GTO 02 118 GTO "PT" 119+LBL "OUT	Output moving avg. Output points	80	
120 RCL 05 121 1 E3 1 122 / 123 1 124 + 125 STO 02 126 RCL 04 127+LBL 05 128 1 129 -	Store counter	90	
130 ENTER† 131 ENTER† 132 RCL 05	Scale pointer	00	

REGISTERS, STATUS, FLAGS, ASSIGNMENTS

DATA REGISTERS			STATUS						
00	k + 1 data array pointer counter	50	EN(.	+ TOT. F FIX RAD	sc	ા	USER M	ODE OFF
05	pointer n_1 is also n_{max}	55	#	INIT S/C	SET IN		AGS s	CLEAR IN	DICATES
	pointers		22		data			no data	
***	n ₂		29	ļ	decimal			no decim	
10	data	60							
	data	00							
	data			<u> </u>					
	:								
				<u> </u>					
15		65						· · · · · · · · · · · · · · · · · · ·	
20		70							
25		75	 						
		_/3							
		-							
30		80							
									 -
_									
35	-	85							
_									
					AS	SIGN	IMEN	TS	
				UNCT		KEY		UNCTION	KEY
10		90	- - '	3.101				CHCHON	NET
									
\Box									†
									1
_									
15		95							
\dashv									
\dashv			 						
									<u> </u>

GOMPERTZ CURVE TREND ANALYSIS

A useful curve for evaluating sales trends, etc., is the Gompertz curve. This is a "growth" curve having a general "S" shape and may be used to describe series of data where the early rate of growth is small, then accelerates for a period of time and then slows again as the time grows long. The sales curves for many products follow this trend during the introductory, growth and early mature phases.

The data points to be fit to a Gompertz curve should be equally spaced along the X (or time) axis and all the data points must be positive. The points are divided serially into 3 groups for data entry.

This program processes the data, fits it to a Gompertz curve and calculates extimated values for future data points. The 3 constants (a,b,c) which characterize the curve are available if desired.

Equations:

$$b = \left(\frac{s - s}{\frac{3 - 2}{s - s}}\right) \frac{1/n}{s}$$

$$c = \exp \left[\frac{1}{n} \left(\frac{\frac{s + s - s^{2}}{1 + s - 2s}}{\frac{1 + s - 2s}{2}} \right) \right]$$

$$a = \exp \left[\frac{(b-1) (s - s)}{b (b^{n} - 1)^{2}} \right]$$

where s_1, s_2 , and s_3 are:

$$s_1 = \sum_{i=1}^{n} l_i y_i = nl_i + b(l_i) \frac{b^{n-1}}{b-1}$$

$$s_2 = \sum_{i=n+1}^{2n} lny_i = n lnc+b^{n+1} (lna) \frac{b^n-1}{b-1}$$

$$s_3 = \sum_{i=2n+1}^{3n} l_{ny_i} = nl_{nc+b}^{2n+1} (l_{na}) \frac{b^{n-1}}{b-1}$$

Example:

The X-Presso Company marketed a revolutionary new coffee brewing maching in 1968. Sales grew at a steady pace for several years then began to slow. The sales records for the first 9 years of the product's life were as follows:

<u>Year</u>	Sales (\$K)	Year	Sales (\$K)
1	18	6	260
2	41	7	282
3	49	8	322
4	151	9	340
5	188		

What are the projected sales volumes for this product in its 10th and 12th year? What is the maximum yearly sales volume for this product if the present trend continues? What annual sales rate would the curve have predicted for the 5th year of the product's life? (Arrange the data as follows)

Group I	Group II	Group III
18	151	282
41	188	322
49	260	340

Keystrokes:	Display:	
[USER]		(Set USER mode)
[XEQ] [ALPHA] SIZE [ALPHA] 007		(occ oblic mode)
[XEQ] [ALPHA] GOMP [ALPHA]	0.0000	
18 [A] 41 [A] 49 [A]	3.0000	
151 [B] 188 [B] 260 [B]	6.0000	
282 [C] 322 [C] 340 [C]	9.0000	(Total # of entries)
[D]	a=0.0042	(a)
[R/S]	b=0.6456	(b)
[R/S]	c=373.9220	(c)
10 [E]	Y.=349.0896	(\$K sales in 10th year)
12 [E]	Y.=363.3649	(#K sales in 12th year)
100 [E]	Y.=373.9220	(Maximum annual sales after long product life)
5 [E]	Y.=202.5965	(\$K sales in 5th year-actual sales were \$188K)

SIZE: 007 **FUNCTION** DISPLAY INPUT STEP **INSTRUCTIONS** [USER] Load program and set USER mode 1. 0.0000 [XEQ] COMP 2. Initialize #of entries Group 1 [A] Key in the first group of data. 3. #of entries Group 2 [B] Key in the second group of data. 4. #of entries Key in the third group of data. [C] Group 3 5. [D] a= Compute coefficients. 6. b= [R/S] [R/S] [E] у •= Compute estimated value y х 7.

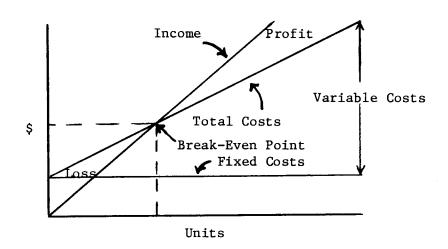
01+LBL "GOM	Initialize	51 -	
F"	initialize	52 /	
02 0		53 RCL 00	
03 STO 00	1	54 /	
04 STO 01	1	55 E1X	1
05 STO 02	1	56 STO 06	†
06 STO 03	1	57 RCL 05	
07 SF 21]	58 1	
08 RTN	1	, 59 -	†
09+LBL A] .	60 RCL 05	1
10 LN	Accumulate	61 RCL 00	1
11 ST+ 01 12 GTO 00	variables	62 Y↑X	
13+LBL B		63 1	1
13 VLBL B		64 -	
15 ST+ 02		65 X12	1
16 GTO 00		66 /	1
17+LBL C		67 RCL 05	i
18 LN		69 RCL 02	
19 ST+ 03	1	70 RCL 01	
20+LBL 00	<u> </u>	71 -	
21 1		72 *	
22 ST+ 00		73 E1X	
23 RCL 00		74 STO 04	
24 RTN		75 "a"	
25+LBL D		76 XEQ 01	
26 3 27 ST/ 00	Compute a,b,c	77 "b"	
27 31/ 00 28 RCL 03		78 RCL 05	
20 RCL 03		79 XEQ 01	
30 -		80 "c"	
31 RCL 02		81 RCL 06 82+LBL 01	
32 RCL 01		83 "F="	Output routine
33 -		84 ARCL X	Tarpar Isaacane
34 /		85 AVIEW	
35 RCL 00		86 RTH	1
36 1/X		87+LBL E	
37 Y1X		88 RCL 05	Compute
38 STO 05		89 X<>Y	Compute y
39 RCL 01		90 Y1X	
40 RCL 03		91 RCL 04	
41 * 40 BC(82		92 X<>Y	
42 RCL 02 43 X↑2		93 Y1X	
43 A12 44 -		94 RCL 06	
45 RCL 01		95 *	
46 RCL 03		96 "Y." 97 XEQ 01	
47 +		97 AEG 61 98 .END.	
48 RCL 02			
49 2			
., 50 *		00	
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REGISTERS, STATUS, FLAGS, ASSIGNMENTS

DATA REGISTERS		DATA REGISTERS	STATUS	STATUS		
00	n s ₁ s ₂	50	SIZE TOT. REG USI ENG FIX SCI ON DEG RAD GRAD	ER MODE X OFF		
05	 	55	FLAGS INIT # S/C SET INDICATES CLEA	R INDICATES		
	С		21 Printer enable			
10		60				
15		65				
20		70				
25		75				
30		80				
35		85				
			ASSIGNMENTS			
40		90	FUNCTION KEY FUNCTION	N KEY		
45		95				

BREAK-EVEN ANALYSIS

Break-even analysis is a technique for analyzing the relationships among fixed costs, variable costs, and income. Until the break-even point is reached, at the intersection of the total income and total cost lines, the producer operates at a loss. After the break-even point, each unit produced and sold makes a profit. Break-even analysis may be represented as follows:



Given four of the following variables: fixed costs (F), sales price per unit (P), variable costs per unit (V), number of units sold (U), and gross profit (GP), this program evaluates the remaining variable. To calculate the breakeven values, simply let the gross profit equal zero.

The degree of operating leverage (OL) at a point is defined as the ratio of the percentage change in net operating income to the percentage change in units sold. The greatest degree of operating leverage is found near the break-even point, where a small change in sales may produce a very large increase in profits. This happens because the profits are close to zero near the break-even point. Likewise, firms with a small degree of operating leverage are operating farther from the break-even point, and they are relatively insensitive to changes in sales volume.

The necessary inputs to calculate the degree of operating leverage are fixed costs (F), sales price per unit (P), variable costs per unit (V), and number of units (U).

For subsequent calculations, it is necessary only to input new data.

Break Even Analysis

$$GP = U(P-V) - F$$

$$OL = \frac{U(P-V)}{U(P-V) - F}$$

Example 1: The Cooper Company sells finance textbooks at \$13 each. Given costs and revenues below, how many textbooks must be sold to break even?

FIXED COSTS

Typesetting Graphics production Printing and binding	\$ 4,000 5,000 3,000
Total fixed costs	\$12,000
VARIABLE COSTS PER COPY	
Distribution Commissions Royalties	\$ 1.00 3.75 2.00
Total variable costs per copy	\$ 6.75
Sales price per copy	\$13.00
Royalties Total variable costs per copy	2.00

Example 2: What is the Cooper Company's degree of operating leverage at 2000 units? At 5000 units?

Keystrokes:	Display:	
[USER]		(Set USER mode.)
[XEQ] [ALPHA] SIZE [ALPHA] 007		
[XEQ] [ALPHA] BEA [ALPHA]	FIXED ?	
12000 [R/S]	PRICE ?	
13 [R/S]	VARIABLE ?	
6.75 [R/S]	UNITS ?	
[R/S]	G. PROFIT ?	
0 [R/S]	UNITS=1920.00	
[B]	UNITS ?	
2000 [R/S]	% LEV.=25.00	
[B]	UNITS ?	
5000 [R/S]	% LEV.=1.62	

				SIZE: 007
STEP	INSTRUCTIONS	INPUT	FUNCTION	DISPLAY
1	Key in the program and set USER mode		[USER]	
2	Initialize		[XEQ] BEA	FIXED ?
3	Input 4 of the following: fixed cost;	F	[R/S]	PRICE ?
	price;	Р	[R/S]	VARIABLE ?
	variable cost;	V	[R/S]	UNITS ?
	no. of units;	U	[R/S]	G. PROFIT ?
	and gross profit.	G.P.	[R/S]	FIXED=\$()
3	When prompted for the unknown quantity,			-or- PRICE=\$()
	press [R/S] (make no input). The			-or- VAR.=\$()
	unknown will be calculated automatically			-or- UNITS=()
	when all the data is input			-or- G.P.=()
4	To find percent operating leverage		[B]	UNITS ?
5	Input number of units	U	[R/S]	% LEV.=()

01◆LBL "BEA	Initialize and	45 -	
	input data	46 STO 03	
02 1.1 03 STO 00		47 "VAR."	
· _ · _ · _ · _ · _ · _ · _ · _ ·		48 XEQ 00	Solve for U
04 CF 22		49+LBL 04	56176 161 6
.05 "FIXED ?		50 RCL 01	
		51 RCL 05	
06 XEQ 09		52 +	L. Control of the Con
07 "PRICE ?		53 RCL 02	
		54 RCL 03	
08 XEQ 09 09 "VARIABL		55 - 57 /	
1		56 /	
E ?"		57 STO 04	
10 XEQ 09		58 "UNITS="	I
11 "UNITS ?	1	59 ARCL X	
** VEO 60		60 PROMPT	G 1 C C D
12 XEQ 09 13 "G. PROF		61+LBL 05	Solve for G.P.
		62 RCL 02	
IT ?"		63 RCL 03	:
14 XEQ 09		64 -	
15 GTO IND		65 RCL 04	
06 16 N DI 01	Solve for F	66 *	!
16+LBL 01	50170 102 1	67 RCL 01	
17 RCL 02		68 -	
18 RCL 03		69 STO 05	
19 -		70 "G.P."	
20 RCL 04	·	71 XEQ 00	Solve for OL
21 *		72+LBL B 73 "UNITS ?	BOIVE FOR OH
22 RCL 05		.73 "UNITS ?	
23 -			
24 STO 01 25 "FIXED"		74 PROMPT	
— ··		75 RCL 02	
26 XEQ 00 27+LBL 02	Solve for P	76 RCL 03	
	301ve 101 F	77 -	
		78 *	
		79 STO 06 80 RCL 06	
31 RCL 04 32 /		81 RCL 01 82 -	
32 / 33 RCL 03		83 /	
33 KCL 63		83 / 84 "% LEV.=	
35 STO 02		84 % LEV	
35 510 02 36 "PRICE"		85 ARCL X	
36 FRICE		86 PROMPT	
38+LBL 03	0.1 6 **	87+LBL 00	Display routine
39 RCL 02	Solve for V	88 "F=\$"	
40 RCL 01		89 ARCL X	
41 RCL 05		90 PROMPT	
42 +	•	91 RTN	
43 RCL 04		92+LBL 09	Input storage
44 /		93 PROMPT	routine
44 /	L	JO FRUNTI	<u> </u>

94 STO IND	51	T
00		-
95 RCL 00	<u> </u>	4
96 FC?C 22	<u> </u>	
97 STO 06	 	ļ
98 ISG 00		
99 RTN		
100 .END.		1
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REGISTERS, STATUS, FLAGS, ASSIGNMENTS

DATA REGISTERS				STATUS					
00	pointer F P	50	ENG	à	TOT. FIX RAD _	2 sci		USER MO ONX_	OFF
05	V U G.P. subroutine pointer	55	# 22		SET IN		3	CLEAR INC	DICATES
10		60							
15		65							
20		70							
25		75							
30_		80							
35		85							
				<u> </u>	<u> </u>	ASSIGN	IMENT	ITS	
40		90		FUNC	TION	KEY	FU	NCTION	KEY
-									
45		95							

EXPERIENCE (LEARNING) CURVE FOR MANUFACTURING COST

Many production process costs vary with output in close relation to the learning curve:

$$C_n = C_1 n \frac{\log r/\log 2}{n}$$

where

 ${\displaystyle \mathop{\text{\rm C}}_{\quad \ \, 1}}$ is the cost of the first unit produced

 ${\scriptsize C}_{\scriptsize n}$ is the cost of the nth unit produced

n is the number of units produced

r is the learning factor

This program solves for any of the above variables and also solves for the average cost over a range from i to j using the formula:

$$\overline{C}_{n} = \frac{C_{1}}{j-i} \qquad \frac{j^{B+1} - i^{B+1}}{B+1}$$

where $B = \log r / \log 2$

The theory applies to a single product, or closely related series of similar products developing through the evolutionary process. The average cost is approximate because of the finite, discrete nature of the function. Small values of i may produce incorrect results.

Example:

A computer manufacturer begins a pilot run on a component. Cost accounting informs him that the first unit off of the line cost \$975 and the 100th unit a week later costs \$643. What cost can the manufacturer expect for the 10,000th unit of the line? What is the average cost of the 10,000 units?

Keystrokes:	Display:	
[USER]		(Set USER mode)
[XEQ] [ALPHA] SIZE [ALPHA] 008		
[XEQ] [ALPHA] LEARN [ALPHA]	0.00	
975 [A]	COST1=975.00	
100 [D]	N=100.00	
643 [C]	COSTN=643.00	
[B]	R=0.94	(Learning factor)
10000 [D]	N=10,000.00	
[c]	COSTN=424.05	(10,000 unit cost)
[ENTER+]	1.00	
10000 [E]	AVG\$=466.13 ((Average for 10,000 units)

	<u></u>			SIZE: 008
STEP	INSTRUCTIONS	INPUT	FUNCTION	DISPLAY
1.	Load program and set USER mode		[USER]	
2.	Initialize		[XEQ] LEARN	0.00
3.	Input three of the following:			
	cost of the first unit	c ₁	[A]	COST 1=
_	learning factor	r	[B]	R=
	cost of the nth unit	C _n	[C]	COST N=
	number of units	n	[D]	N=
4.	Compute the remaining variable:			
	cost of the first unit	·	[A]	COST 1=
	learning factor		[B]	R=
	cost of the nth unit		[C]	COST N=
	number of units		[D]	N=
5.	Compute the average cost from the ith			
	to the jth unit	i	[ENTER]	
		j	[E]	AVG\$=

Ø1+LBL "LEA	Initialize	51 Y1X	
RN"		52 RCL 01	
02 CF 22		53 *	1
03 FIX 2		54 STO 03	
04 SF 21		55 GTO 02	
05 CLX	1	56+LBL D	
06 RTN	1	57 "N"	
07◆LBL A	1	58 STO 04	
08 "COST1"		59 FS?C_22	
09 STO 01	1	60 GTO 02	
10 FS?C 22		61 RCL 02	Calculate n
11 GTO 02		62 XE0 00	
12 RCL 02	Calculate Cost 1	63 2	
13 XEQ 01	$\left(C_{1}\right)$	64 1/X	
14 RCL 04	1	65 +	
15 X<>Y		66 INT	
16 Y†X	,	67 STO 04	
17 RCL 03	1	68 GTO 02	1
18 X<>Y		69+LBL 01	
19 /		Z0 LOG	
20 STO 01		71 2	B=log r/log ²
21 GTO 02		72 LOG	2 106 17106
22 RTN	1	73 /	
23+LBL B		74 RTN	1
24 "R"		75+LBL E	
25 STO 02		76 "AVG\$"	
26 FS?C_22	1	77 STO 05	Calculate \overline{C}_n
27 GTO 02		78 RCL 02 79 XEQ 01	n n
28 RCL 04	Calculate r		
29 XEQ 00		80 1 81 +	
30 STO 02	+	82 STO 07	
31 GTO 02		83 Y1X	
32+LBL 00		84 X<>Y	
33 XEQ 01		85 STO 06	
34 RCL 03		86 RCL 07	
35 RCL 01		87 Y1X	
36 ∕ 37 LOG		88 -	
37 EUG 38 X<>Y		89 RCL 07	
39 /	1	90 /	
39 / 40 101X	1	91 RCL 01	
40 101A 41 RTN		92 *	
41 KIN 42+LBL C	!	93 RCL 05	
42 "COSTN"	·	94 RCL 06	
44 STO 03	1	95 -	
45 FS?C 22	†	96 /	
46 GTO 02	†	97 ♦ LBL 02	
47 RCL 02		98 "h="	
48 XEQ 01	Calculate Cost n	99 ARCL X	
49 RCL 04	(C)	100 AVIEW	1
50 X<>Y	(C _n)	101 .END.	
	1		

REGISTERS, STATUS, FLAGS, ASSIGNMENTS

	DATA REGISTERS	STATUS
00 C r C C C C C C C C	50	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$
n 05 i ; Cn i	55	FLAGS INIT # S/C SET INDICATES CLEAR INDICATES
B+1		22 Digit entered
0	60	
5	65	
0	70	
	70	
5	75	
)	80	
	85	
		ASSIGNMENTS
)	90	FUNCTION KEY FUNCTION KEY
	95	
	30	

PRICE ELASTICITY OF DEMAND

Using historical (or estimated)prices and resulting unit sales, this program calculates the elasticity of demand (elasticity of quantity sold with respect to a change in price).

Equations:

$$E_{d} = \frac{\Delta Q}{\frac{1}{2}(Q_{i} + Q_{i+1})} \frac{\Delta P}{\frac{1}{2}(P_{i} + P_{i+1})}$$

where:

$$E_d = demand elasticity$$

$$Q_{i+1}$$
 = quantity sold after price change

$$Q_{i}$$
 = quantity sold before price change

$$P_{i+1} = \text{new price}$$

$$P_i = old price$$

$$i = 1,2,3,..., n$$

$$\Delta Q = Q_{i+1} - Q_i$$

$$\Delta P = P_{i+1} - P_{i}$$

$$\frac{\Delta P}{\frac{1}{2}[P_{i} + P_{i+1}]} \neq 0$$

Example:

The sales volume of a product varied with the different price changes per unit as follows:

<u>N</u>	Quantity sold (Q)	Price/Unit (P)
1	0	6
2	10	4
3	20	2
4	30	0*

Compute the price elasticity of demand.

*hypothetical price for simplicity

Keystrokes:	Display:

	Dispidy.
[XEQ] [ALPHA] SIZE [ALPHA] 005	
[XEQ] [ALPHA] DEMAND [ALPHA]	PRICE=?
6 [R/S]	QUANTITY=?
0 [R/S]	PRICE=?
4 [R/S]	QUANTITY=?
10 [R/S]	Ed=5.0000
[R/S]	PRICE=?
2 [R/S] 20 [R/S]	Ed=1.0000
[R/S]	PRICE=?
0 [R/S] 30 [R/S]	Ed=0.2000

SIZE: 005

				005
STEP	INSTRUCTIONS	INPUT	FUNCTION	DISPLAY
1.	Load program			
2.	Initialize		[XEQ] DEMAND	PRICE=?
3.	Key in first price of series	Price 1	[R/S]	QUANTITY=?
4.	Key in first quantity of series	Quantityl	[R/S]	PRICE=?
5.	Key in subsequent price	Price n	[R/S]	QUANTITY=?
6.	Key in subsequent quantity and calculate			
	demand elasticity	Quantityn	[R/S]	Ed=
7.	Press [R/S] to return to step 5 to enter			
	next price		[R/S]	PRICE=?
8.	For a new case, go to step 2.			
				•
	·			
				1

_			
01+LBL "DEM	Initialize	51	
AND"	Interactive		
02 SF 21 03 XEQ 03			
03 AE0 03 04 STO 02			
05 XEQ 04			
06 STO 04			
07+LBL 00			
08 XEQ 03 09 X(> 02	Shift data		
10 STO 01	billic data	60	
11 XEQ 04			
12 X(> 04 13 STO 03			
13 3 (0 93			
15 STO 00			
16*LBL 01			
17 XEQ 02 18 DSE 00	Calculate E		
18 DSE 00 19 GTO 01	a		
20 /		70	İ
21 CHS			
22 "Ed="			
23 ARCL X 24 AVIEW			
25 GTO 00			
26+LBL 02			
27 RCL IND 00			
28 ENTER↑			
29 DSE 00		80	
30 RCL IND			
00 31 -			
32 X<>Y			
33 LASTX			
34 +	!		
35 / 36 RTN			
37 ♦ LBL 03			
38 "PRICE=?	Prompting	90	
	Prompting subroutines		
39 PROMPT 40 RTN			
41+LBL 04			
42 "QUANTIT			
Y=?"			
43 PROMPT 44 .END.			
44 • CHD•			
		00	

REGISTERS, STATUS, FLAGS, ASSIGNMENTS

DA		STATUS						
OO USED PiPi+1	50	ENG		5 TOT FIX _ RAD	so	CI	USER M ON	ODE X
05 Q _{i+1}	55	#	INIT S/C	SET I		AGS	CLEAR IN	DICATES
		21		Printer				
10	60							
15	65							
20	70							
25	75							
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					ASSIG	NMEN	TS	
		F				F	UNCTION	KEY
40	90							
45	95							

HP-41C

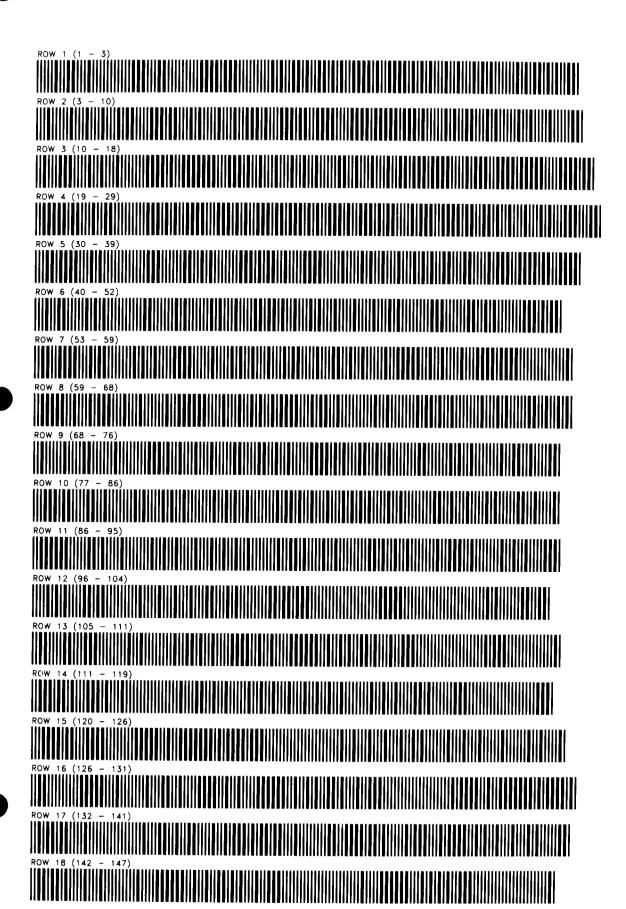
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BUSINESS STAT/MARKETING/SALES

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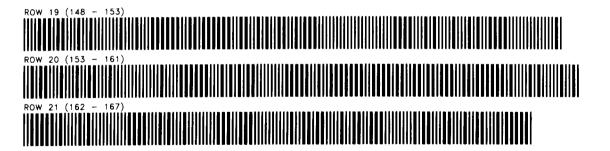
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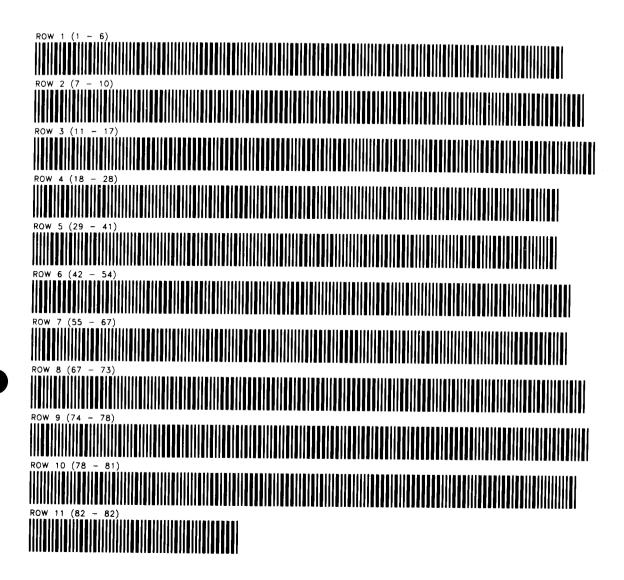


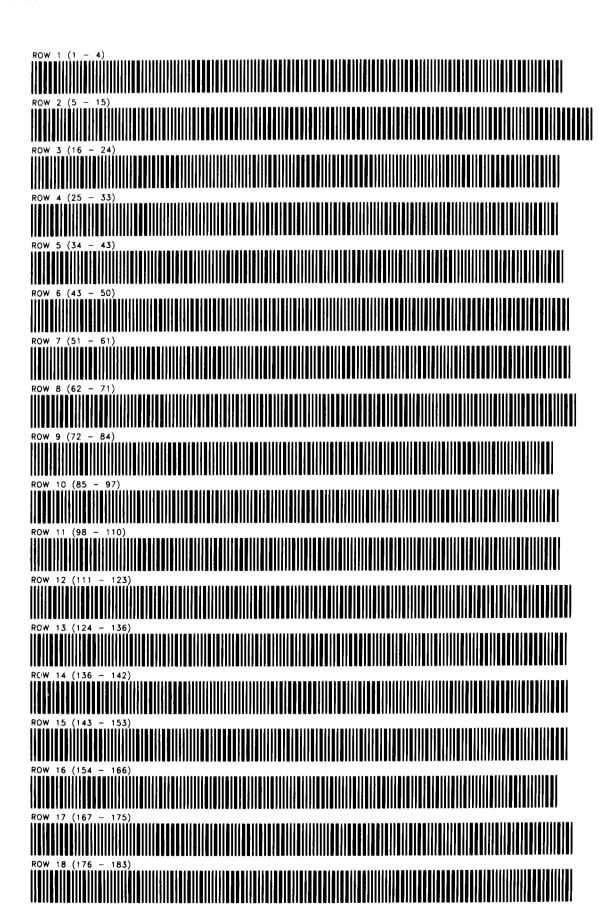
1

FORECASTING USING EXPONENTIAL SMOOTHING



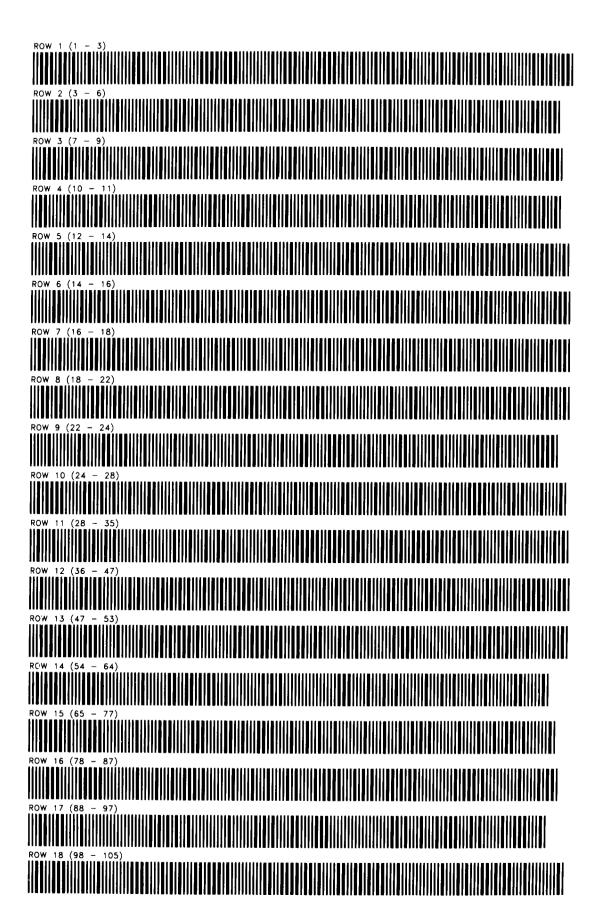
MONTHLY SEASONAL VARIATION FACTORS — CENTERED MOVING AVGS PROGRAM REGISTERS NEEDED: 19



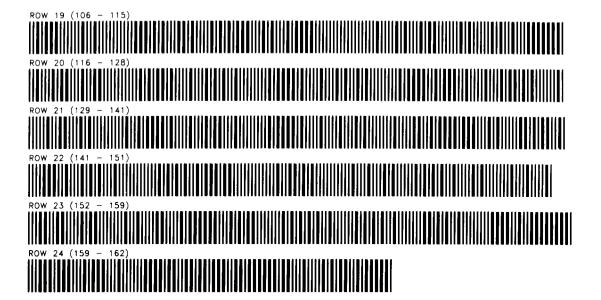


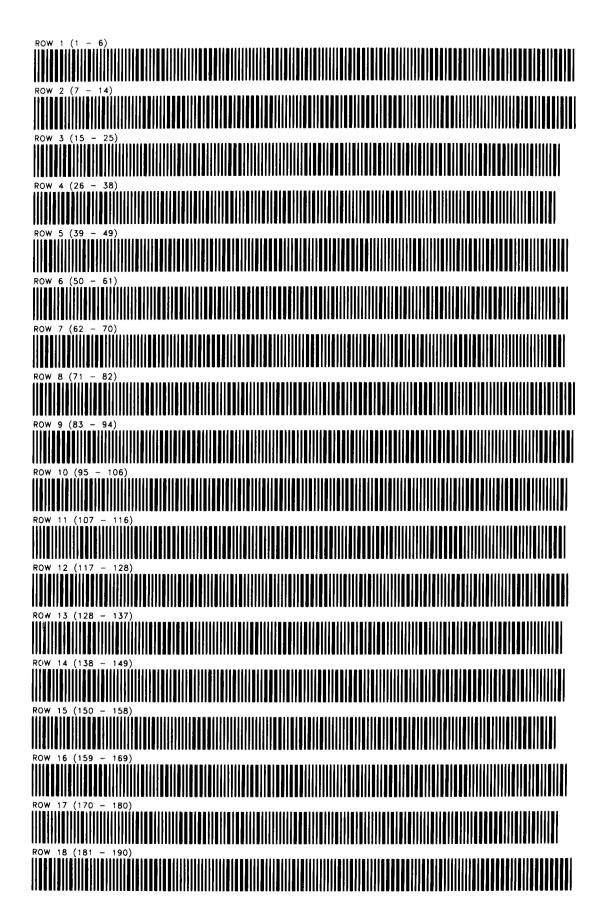
MULTIPLE LINEAR REGRESSION





NORMAL AND INVERSE NORMAL DISTRIBUTIONS



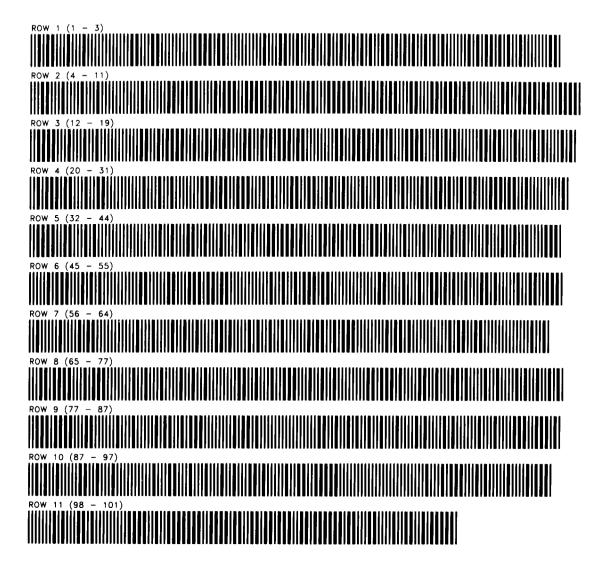


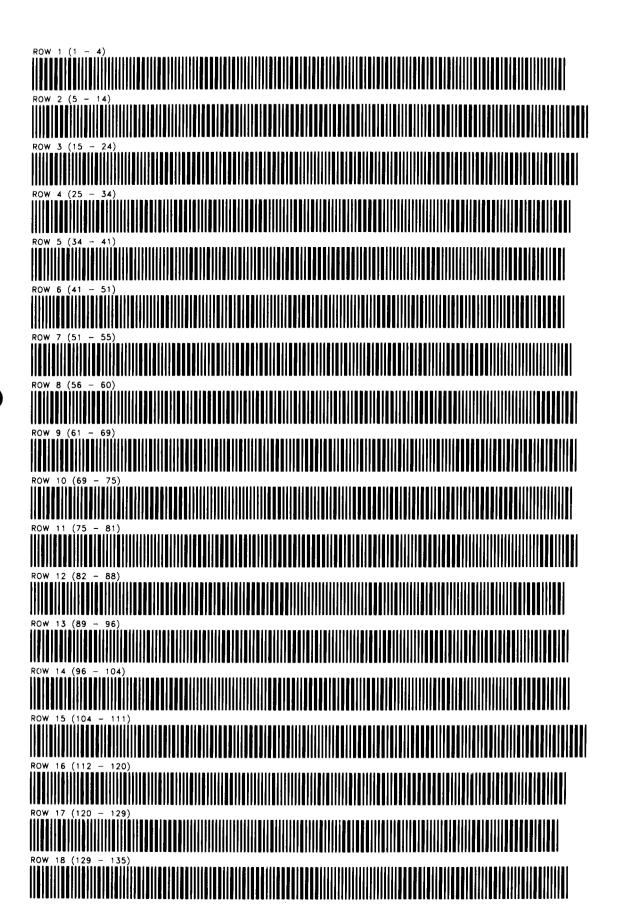
8

T DISTRIBUTIONS



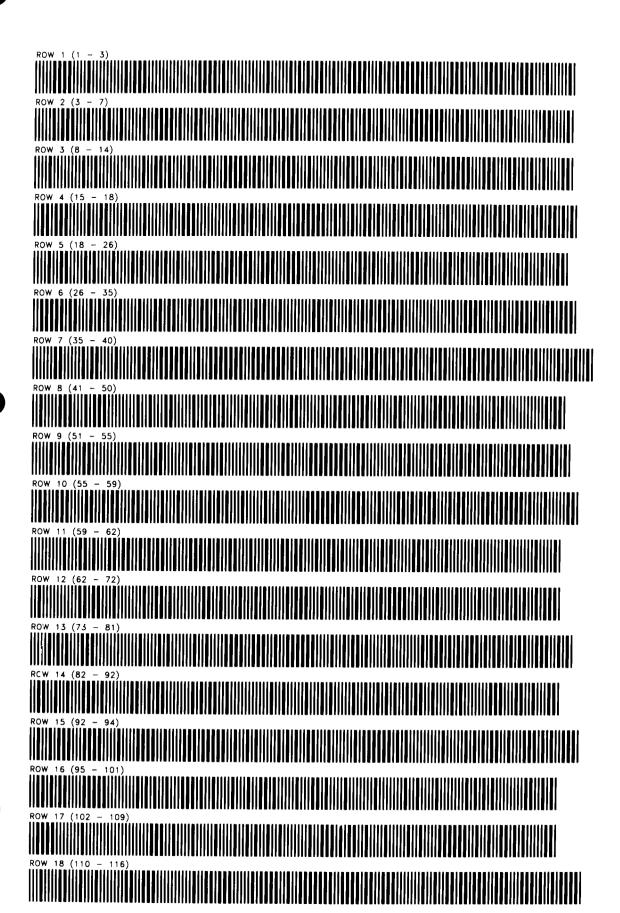
F DISTRIBUTIONS

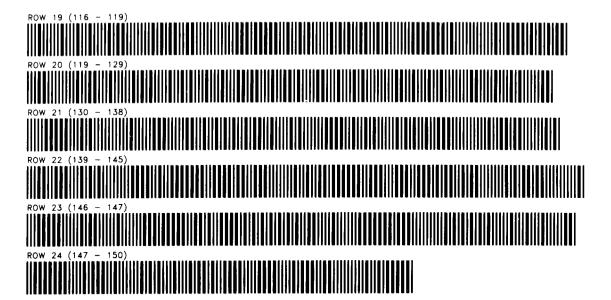




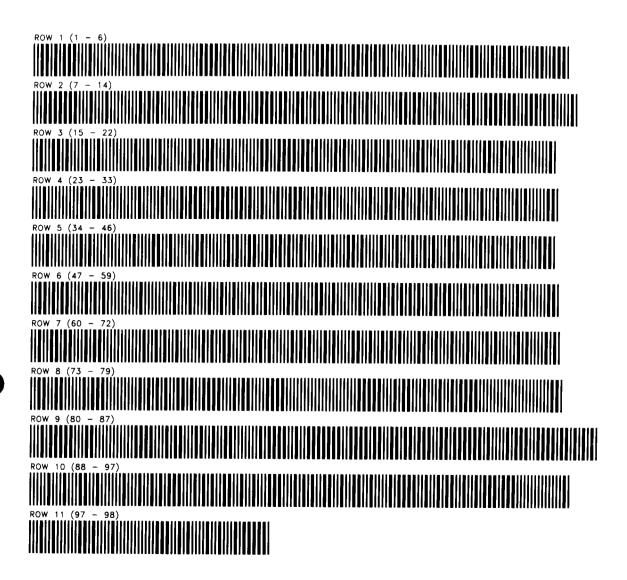
BASIC STATISTICS FOR TWO VARIABLES

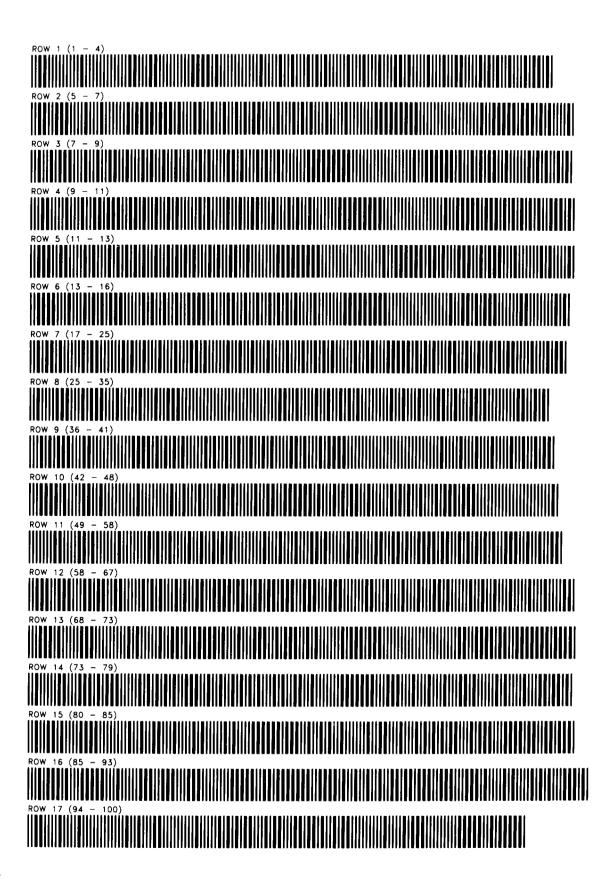
ROW 19 (136 - 140)

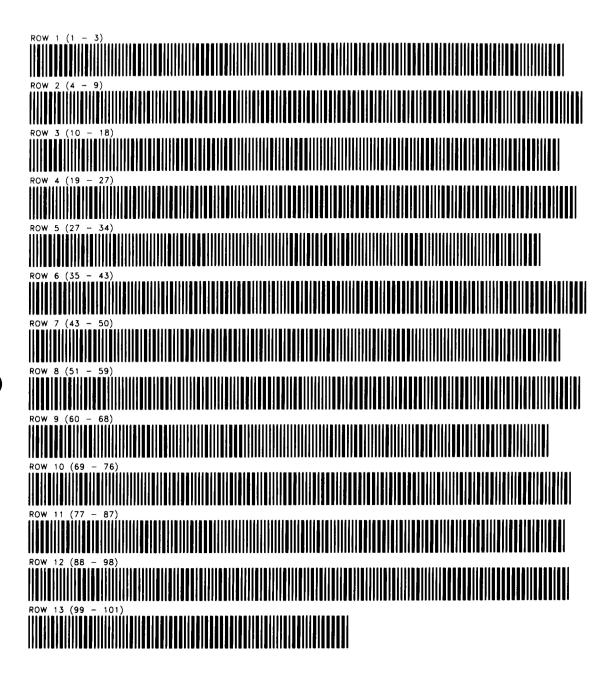




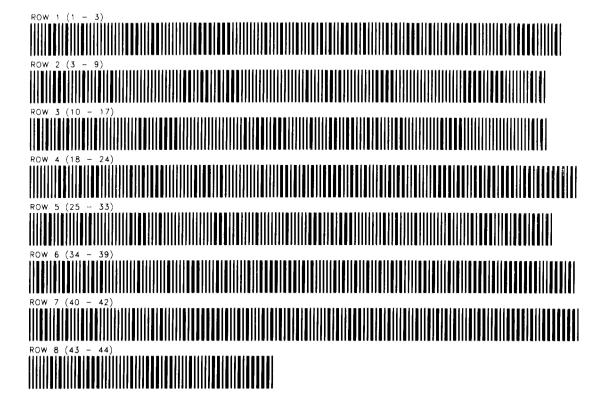
GOMPERTZ CURVE TREND ANALYSIS







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Physics
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^{*} Some books require additional memory modules to accomodate all programs.

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MONTHLY SEASONAL VARIATION FACTORS BASED ON CENTERED
MOVING AVERAGES
MULTIPLE LINEAR REGRESSION
NORMAL, INVERSE NORMAL, T AND F DISTRIBUTIONS
BASIC STATISTICS FOR TWO VARIABLES
MOVING AVERAGE
GOMPERTZ CURVE TREND ANALYSIS
BREAK-EVEN ANALYSIS
EXPERIENCE (LEARNING) CURVE FOR MANUFACTURING COST
PRICE ELASTICITY OF DEMAND

